Menoufeya University College of Engineering Civil Engineering Dpt.



Finite Element 600 M. Sc. Jun. 2017 Time allowed 3 hrs

OPEN BOOK

<u>Question (1) (20 %)</u>

Two straight bars ab and bc are pinned together as shown. Bar bc is cooled 40° C. Determine the displacement at b and the force in each bar. Thermal expansion coefficient $\alpha = 1.2 \times 10^{-5} \text{ mm/mm} \,^{\circ}\text{C}$, E 200,000.0 MPa.

Question (2) (20 %)

Figure 2 shows two-member plane truss supported by a linearly elastic spring. The truss members are of solid circular cross section having d=20 mm and E=80 GPa. The linear spring has stiffness constant 50 N/mm.

- a- Assemble the system global stiffness matrix and calculate the displacements at b.
- b- Calculate the reactions at a and c.
- c- Calculate the strain and stress in each bar.

<u>Question (3) (20%)</u>

For the beam shown in figure, use the stiffness method to :

- a- Calculate the rotations at B.
- b- Calculate the reactions at A and C.
- c- Draw the shearing force and bending moment diagrams for the beam.

 $E = 200 \text{ GPa}, I = 50 \times 10^{-6} \text{ m}^4.$

Question (4) (20 %)

Analyze the grid shown in figure. The grid is fixed at nodes 1 and 3, and is subjected to a downward vertical load of 24 kN. The global coordinate axes and element lengths are shown in figure. each member have the following property : E=210 GPa, G=84 GPa, $I=16 \times 10^{-5} \text{ m}^4$, $J=5 \times 10^{-5} \text{ m}^4$

Question (5) (20 %)

Using the finite element method to:

- a- Calculate the approximate first buckling load for a cantilever beam of length L=3.0 m, and EI=16 $\times 10^3$ kN.m².
- b- Calculate the tip deflection and rotation of the cantilever beam when subjected to distributed transverse load of 12 kN/m along with a compression load of 1800 kN.
- c- Compare the values of (b) with the values when P=0.



Question (5)