Menoufiya University **Faculty of Engineering** Shebin El- Kom Second (June) Term Examination Academic Year: 2014-2015 Date: 13/6/2015

**Minuflya University** 

**Dept.: Production Engineering** Year : Master Subject: Dynamic of Multi-bodies systems Code : PRE 619 **Time Allowed: 3 hours** Total Marks : 100 Marks

Allowed Tables and Charts: None Examiners: Dr/ Mohamed Hesham Belal Answer All the Following Questions:

### Question No.(1):

(a)- For the shown 2-DOF vibrating system in Fig.(1), all data are given. Determine the equations of motion using Lagrange's equation.

- (b)- For the shown framed structures in Fig.(2), assuming the axial deformation of all members are neglected and all data are given. The force acting on the joints A and B are given respectively F<sub>1</sub>, F<sub>2</sub>, M<sub>3</sub>, F<sub>4</sub>, F<sub>5</sub>, M<sub>6</sub> as shown.
  - (1)- Derive the form of the holonomic scleronomic constraints subjected to the frame.
  - (2)- Derive the expression of the generalized forces.

### Question No.(2):

- (a)- The forces of multi-body systems can be classified mainly into three types. Discuss this statement.
- (b)- A sphere of radius R rolls without sliding on the horizontal surface as shown in Fig.(3). Write down the equation of scleronomic constraints and non-scleronomic constraints.
- (c)- Derive the Hamilton's canonical equations of the shown system in Fig.(4). All data are given.

## Question No.(3):

- (a)- There are three approaches of condensation process for reducing the number of generalized coordinates describing the kinematic configuration of large multi-body systems. Write down in brief the process for each approach.
- (b)- A trailer is modeled by 3-DOF system as shown in Fig.(5). All data are given.
  - (1)- Determine the equations of motion using Lagrange's equation,
  - (2)- Use condensation technique to derive the equation of vertical motion of the trailer.

## Question No.(4):

- (a)- From the first principle, Derive the expressions of the mass and stiffness matrices for the single element in terms of the global reference system.
- (b)- Fig.(6) shows the single flexible link manipulator of uniform cross-section diameter D, length L, mass per unit volume  $\rho$  and Young's Modulus E. The manipulator having flexible joint  $O_1$  of stiffness coefficient (k<sub>F</sub>) and payload of mass (m<sub>P</sub>) welded at the tip of the link. (1)- Write the local mass and stiffness matrices,
  - (2)- Derive the global mass and stiffness matrices,
  - (3)- Write-down the equation of motion of the manipulator in detail, and
  - (4)- Calculate the equivalent joint torque acting at the shoulder joint.

## [25 Mark]

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Fig.(6)

With my best wishes

This exam measure the following ILOs											
Question No.	Q2-a	Q3-a	Q4-a	Q1-b	Q2-b	Q3-b	04-b	01-b	02-c	03-h	04-b
	a-1	a-3	a-6	b-1	b-6	b-1	b-6	c-4	c-3	c-3	C-4
Skills	Knowledge & Understand			Intellectual				Professional			

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