EL-Menoufia University Faculty of Engineering – Shebin EL-Koum The Final Exam of The Second Term 2017-2018 Engineering Mathematics For The Prep. Year

Date: 2-6-2018 Marks: 100

Time: 3 Hrs.

Answer All the following questions:

Q1: (24 Marks) 1- prove that $\int e^{ax} \cosh bx \, dx = \frac{e^{ax}}{b^2 - a^2} \left[b \sinh bx - a \cosh bx \right] + C$ 2- Evaluate the following integrals: (i) $\int \frac{dx}{\sin x - \cos x + 1}$ (ii) $\int \frac{dx}{(1 + \sqrt{x})\sqrt{x - x^2}}$ (iii) $\int_{0}^{1} \frac{\ln(1 + x)}{1 + x^2} \, dx$ (iv) $\int \frac{x^{-3} - 6x^2 + 11x - 6}{\sqrt{x^2 + 4x + 3}} \, dx$ (v) $\int x^{-11} (1 + x^4)^{-\frac{1}{2}} \, dx$ Q2: (26 Marks)

(a) Using integration, find the volume and the surface area generated when the region bounded by the following curves: x = 2 - |y - 2| and x = 0 is rotated about the x-axis.

(b) Calculate the length of the arc of the curve $y = \frac{1}{6}(x^3 + \frac{3}{x})$ between x = 1 and x = 3. (5 Marks)

(c) Find the area bounded by the curves $y = x^2 - 6x + 8$ and y = 2x - 7.

(5 Marks)

(12 Marks)

(d) Use Simpson's rule to approximate $\int_{a}^{1} \sqrt{x + x^2} dx$, using 4 subintervals. (4 Marks)

<u>Q3</u>:

(50 Marks)

- (a) Prove that the equation $2x^2 + 7xy + 3y^2 + 8x + 14y + 8 = 0$ represents two straight lines. Find the two lines, the angle between them, and bisector equations.
- (b) By suitable transformation of cordinate axes, remove first degree term of the equation $x^2 4xy + 3y^2 + 6x 8y + 15 = 0$, then classify the obtained equation.
- (c) Discuss and sketch the hyperbola $9x^2 16y^2 + 18x + 32y 151 = 0$, then find the foci, directrices, and asymptotes.
- (d) If the normal at the end of a latus rectum of an ellipse passes through one extremity of the minor axis, show that the eccentricity of the curve is givin by the equation $e^4 + e^2 1 = 0$.
- (e) Find the equation of the common tangent of $y^2 = 8x$ and $x^2 = 12y$.
- (f) Sketch the graph of the polar equation $r^2 = 4r \cos \theta$, then transform it into Cartesian coordinates.

Good Luck