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# Digital Simulation of Optimum PWM Inverter Control Asynchronous Motor

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#### **Abstract**

This paper deals with a digital closed loop speed control of 3-phase induction motor fed by Pulse Width Modulation (PWM) inverter using microprocessor technique. The proposed control relies on a simplified algorithm to compute the optimum switching instants of PWM inverter and the frequency of input voltage to the motor. Starting transients as well as steady state performance of the system including disturbance in load torque, step change in speed reference and step change in torque reference have been studied.

#### Keywords:

Optimum PWM Inverter, Asynchronous motor, Microprocessor

#### 1. Introduction

Siala and others show that induction motors are widely used in industrial applications due to their attractive price and robustness and consequently, the demand for high-performance control strategies for asynchronous drives is always increases /1/.

The control of electric drives was traditionally carried out by means of analogue devices. It, therefore, benefits of the support of traditional theories of automatic controls. A large technical literature has been made in life. Well-known mathematical methods have been proposed to contribute the theoretical solutions for many practical problems. The production of microprocessor and their

quick development, combined with the continuos reduction of their computing time, make now possible a widespread use of fully digitalized controls for the solution of control problems in electric drives /2/.

Bowes and others indicate that microprocessor control of power-electronic equipment offers the possibility σf improvements in manufacture. realiability, maintenance, servicing and increased control flexibility. These advantages inevitably result from a reduction in the complex control circuitry which may be progressively replaced by microprocessor software. It is then possible to change the drive characteristics without altering the hardware. An overview of a possible control hierarchy and distinguishes some of the more desirable features associated with PWM variable speed drive systems /3/.

The speed control of the polyphase induction motor is an art that has attracted a good deal of study in recent years. A number of techniques have been developed to utilize their data processing power to control PWM inverter. The natural PWM process, which is based on the analog comparison of a sinusoidal signal and a triangular signal, takes place in real time. This process is believed to be unsuitable for efficient microprocessor implementation, because of insufficient speed of the presently available microprocessors. As a consequence, various digital methods, such as 'regular-sampled PWM' and 'optimal PWM' techniques, have been developed specifically to suit microprocessor-based implementation /4/.

This paper develops a reasonable digital simulation of PWM inverter control asynchronous motor to check the starting-up and steady state performance of the motor.

#### 2. Optimum Pulse Width Modulation (PWM) inverter model

In microprocessor implemented PWM control schemes /5/, it is very important to develop an efficient and simple model for desired performance.

In the controllers of PWM inverter, it is easy to implement the digital modulation technique. This technique indicates the selection of the switching angles of the inverter output voltage, in such a way that this voltage fulfils given condition. Among the digital techniques, the harmonic technique and that of the optimum waveform

are the most common, a typical voltage waveform of the input PWM voltage inverter is shown in Fig.1, it exhibits quarter wave and half-wave symmetry (M=3), the switching pattern  $\alpha$  satisfies the following relations:

$$0 < \alpha_1 < \alpha_2 < \alpha_3 \quad ---- \quad \alpha_M < \pi/4 \quad ---- \quad (1)$$

The  $r-\underline{th}$  harmonics of the waveform of Fig.1, is equal to :

#### M+1

$$V_r = \frac{4E}{\pi r} \left( 1 - 2 \sum_{i=1}^{r} (-1)^{i+1} \cos(r \alpha_i) \right)$$

The constraints imposed on  $\alpha$  by the harmonic elimination technique, for each r th harmonics to be eliminated are:

$$\Gamma \neq 1$$
,  $\forall r(\alpha)=0$  \_\_\_\_\_(3)

#### M+1

$$V_1 = \frac{4E}{\pi} \left( 1 - 2 \sum_{i=1}^{\infty} (-1)^{i+1} \cos(\alpha_i) \right)$$
 (4)

The solution of the non linear equations 1 ---> 4 requires very complex numerical algorithms. The pulse-widths or switching angles for some levels of the first harmonics of the inverter output voltage can be obtained in off time and stored in the microprocessor memory as a look-up table, the task of obtaining the angles, allows it to operate in real time /6/. The microprocessor acts simply as a pulse generator producing pulses of predetermined widths. With PWM techniques, one look-up table corresponds to a certain magnitude of the inverter output voltage. If the output voltage is to be varied, it becomes necessary to prepare a number of look-up tables each corresponding to a certain output voltage level. The microprocessor is then programmed to switch from one look-up to another in order to change the output voltage magnitude for keeping V/F = constant.

#### 3. The d-q representation of 3-phase induction motor

A 3-phase induction motor supplied by PWM inverter is considered. Neglecting its core losses, saturation effects and space harmonics, the motor can be described by the following set of equations:

| $\Psi_{ds} = L_{s}  _{ds} + L_{sr}  _{dr} - \dots $ (5) $\Psi_{ds} = L_{s}  _{ds} + L_{sr}  _{dr} - \dots $ (6)  |
|--|
| - US - 3 US - 3 UI   |
| $\Psi_{dr} = L_r l_{ds} + L_{sr} l_{ds} \qquad (7) \qquad \Psi_{qr} = L_r l_{qs} + L_{sr} l_{qs} \qquad (8)$   |
| $d\Psi_{ds}/dt = V_{ds} + W_a \Psi_{qs} - R_s I_{ds} \qquad (9)$   |
| $d\Psi_{qs} / dt = V_{qs} - W_a \Psi_{ds} - R_s I_{qs} \qquad (10)$  |
| $d\Psi_{dr}/dt = V_{dr} + (W_{a-}W_{R})\Psi_{qs} - R_{\Gamma}I_{dr} \qquad (11)$   |
| $d\Psi_{qr} / dt = V_{qr} - (W_{a} - W_{R}) \Psi_{ds} - R_{r} I_{qr}$ (12)   |
| $Vds = 2/3 [V_{a} \cos \Theta + V_{b} \cos (\Theta - \frac{2\pi}{3}) + V_{c} \cos (\Theta + \frac{2\pi}{3})] \qquad (13)$                                  |
| $Vqs = 2/3 [V_a \sin \Theta + V_b \sin (\Theta - \frac{2\pi}{3}) + V_c \sin (\Theta + \frac{2\pi}{3})]$ ——— (14)   |
| $V_{dr} = V_{qr} = 0$ (15) S = (W <sub>e</sub> - PW <sub>m</sub> )/W <sub>e</sub> (16)   |
| $T_e = 3/2 P L_{sr} [l_{qs} l_{dr} - l_{ds} l_{qr}] = T_l + KW_m + J dW_m / dt$ (17)   |
| $We = 2 \pi F$ (18) $W_R = PW_m$ (19)  |
| $ids = 2/3 \left[ l_a \cos \Theta + l_b \cos \left( \Theta - \frac{2\pi}{3} \right) + l_c \cos \left( \Theta + \frac{2\pi}{3} \right) \right] \qquad (20)$ |
| $lqs = 2/3 \left[ l_2 \sin \Theta + l_b \sin \left( \Theta - \frac{2\pi}{3} \right) + l_c \sin \left( \Theta + \frac{2\pi}{3} \right) \right] $ (21)       |
| From eqs. (20) & (21) at $\Theta = 0$ lds = la and at $\Theta = 90$ ° $l_{qs} = la$  |
| From eqs. (5) ——> (8), the following simplified Eqs. are   |
| $I_{ds} = [L_{sr}\Psi_{dr} - L_{r}\Psi_{ds}] / [L_{sr}^{2} - L_{s}L_{r}] \qquad (22)$  |
| $l_{qs} = [L_{sr}\Psi_{qr} - L_{r}\Psi_{qs}] / [L_{sr}^{2} - L_{s}L_{r}] \qquad (23)$  |
| $I_{df} = [\Psi_{ds} - L_s I_{ds}] / [L_{sf}] $ (24)   |
| $l_{qr} = [\Psi_{qs} - L_{s}l_{qs}] / [L_{sr}] $ (25)  |
| -dr 1-ds -s-ds) -1-si  |
| The equations 9>25 are solved  |
| numerically using the Runge Kutta method, with a   |

numerically using the Runge Kutta method, with a sufficiently small step length.

#### 4. Basic structure of the control system

A closed-loop system generally has the advantages of greater accuracy, improved dynamic performance and reduced effect of disturbances such as loading. When the drive requirements include rapid acceleration and deceleration, closed loop control is necessary. The basic block diagram of the control system is shown in Fig. 2, the feedback

angular speed of the motor  $(\mathbf{W}_m)$  is compared with the reference angular speed  $\mathbf{W}_{ref}$  and the difference  $\Delta \mathbf{W}_m$  is modified by PI controller algorithm of speed to obtain  $\Delta \mathbf{W}$  which added to  $\mathbf{W}_m$  to obtain  $\Delta \mathbf{e}$  and multiplied by factor  $P/2\pi$  to obtain  $\Delta \mathbf{e}_1$ . The equation of each part of the system is developed as follows:

$$\Delta W_{m}(t) = K_{s} \quad W_{m}(t) + K_{s}/T_{s} \int_{W_{m}(t)}^{t} W_{m}(t) dt \qquad (26)$$

$$\Delta W_{m}(t) = W_{ref} - W_{m}(t) \qquad (27)$$

$$\Delta e(t) = W_{m}(t) + W_{m}(t) \qquad (28)$$

$$\Delta e_{1}(t) = P \quad \Delta e / 2\pi \qquad (29)$$

The rotor speed  $(\mathbf{W}_m)$ , d-c link voltage, stator phase currents and flux can be measured. The electromagnetic torque of the motor is computed from equation (17), and compared with the reference torque  $(T_{ref})$ , the difference between them  $\Delta T$  is modified by the PI controller algorithm to obtain  $\Delta e_2(t)$  which added to  $\Delta e_1(t)$  to obtain the required frequency of PWM inverter. Using a suitable algorithm to select the required look-up table, contains the switching points of optimum PWM inverter (or the required angles  $\alpha_i$ ), d-c link input voltage of the inverter can be controlled to keep E/F= constant.

$$F \leftarrow F_n \& E = V_n \text{ if } F > F_n$$
 (30)

The PI controller of torque can be achieved by the following Equations :

$$\Delta e_{2}(t) = K_{\Gamma} T(t) + K_{\Gamma} / T_{\Gamma} \int_{0}^{t} Wm(t) dt$$

$$\Delta T(t) = T_{ref} - T_{e}(t)$$
(31)

#### 5. Simulation Results

The simulations have been carried out on the motor with the following parameters: full load torque=9.25n.m., rated speed=1418r.p.m., Vn= 310.3 volt., J=0.009kg.m²,  $L_r$ =0.34h,  $L_s$ = 0.34h,  $L_s$ =0.318h,  $R_s$ =4.7 ohm,  $R_r$ = 4.1 ohm, P=2 and for the PI controllers of speed and torque, the

parameters are: K<sub>S</sub>=10, T<sub>S</sub>=0.0001, K<sub>T</sub>=10, T<sub>T</sub>=0.0001, N<sub>Tef</sub>=1410r.p.m., W<sub>Tef</sub>=  $2\pi N_{Tef}/60$ ., T<sub>Tef</sub>=9.5n.m., and for the optimum PWM inverter voltage: no of harmonics elimination=50, V<sub>T</sub>( $\alpha_i$ )=0, r <> 1, M=3,  $\alpha_1$ =0.0785rad.,  $\alpha_2$ =0.196rad.,  $\alpha_3$ =0.2748 rad. The input of the actual motor speed was performed continuously through encoder circuit connect to the microprocessor. The stator phase currents of the motor were connected to microprocessor through A/D circuit.

#### 5.1 Motor starting without controller

Starting-up transient of loaded motor fed by 3-phase optimum PWM inverter has been considered. Fig.3 shows the performance of the motor during transient and steady state periods. The minimum and maximum values of the currents, flux, speed, torque and frequency are as given in Table 1.

|       | min.     | min.  |
|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----------|-------|
|       | and      | and   |
|       | max.     | max.  |
|       | lds    | iqs    | torq.  | idr    | lar    | ₽ds .  | ¥qs    | ₩dr    | ¥qr    | Nr       | freq. |
|       | (emp.) | (amp.) | (n.m.) | (amp.) | (amp.) | (Wb.)  | (Wb.)  | (WD.)  | (WD.)  | (r.p.m.) | (hz.) |
| trans | -28.66 | -23.3  | -3.24  | -21.12 | -23.5  | -1.62  | -1.26  | -1.083 | -1.052 | C        | 50    |
| trans | 21.26  | 24.28  | 52.05  | 25.55  | 22.04  | 1.68   | 1.136  | 1.083  | 1.053  | 1469.4   | 50    |
| S.S.  | -4.46  | -4.596 | 8.123  | -3.055 | -2.814 | -1.159 | -1.115 | -1.081 | -1.052 | 1447.6   | 50    |
| S.S.  | 4.462  | 4.596  | 10.31  | 3.055  | 2.813  | 1.159  | 1.115  | 1.081  | 1.051  | 1448.8   | 50    |

Table 1 Performance of the motor during transient and steady state periods (without controller)

#### 5.2 Motor starting with controller

A desirable approach for control systems is to incorporate all digital control loop. There are many advantages of this approach. The digital control loop eliminates the need for traditional analog compensation circuits and their associated multiplicity of adjustments.

The parameters of closed-loop speed and torque control are: ( $K_s=10$  &  $T_s=0.0001$ ),  $T_{ref}=9.5$  n.m.,  $N_{ref}=1410$  r.p.m.,  $W_{ref}=2\pi$   $\frac{N_{ref}}{60}$ ,  $K_r=10$  and  $T_r=0.0001$ . Fig.4 shows the performance of the motor during the transient and the steady state periods. The minimum and maximum values of the currents, flux, torque, speed and frequency are given in Table 2.

|       | min.<br>and<br>max.<br>Ids<br>(amp. | min.<br>and<br>max.<br>lqs<br>(amp. | min.<br>and<br>max.<br>torq.<br>(n.m.) | min.<br>end<br>mex.<br>Idr<br>(emp. | min.<br>and<br>max.<br>iqr<br>(amp. | min.<br>and<br>max.<br>¥ds<br>(wb.) | min.<br>and<br>max.<br>¥qs<br>(wb.) | min:<br>and<br>max.<br>¥dr<br>(wb.) | min,<br>and<br>max.<br>¥qr<br>(wb.) | rnin.<br>Iand<br>Max.<br>Nr<br>(r.p.m.) | min.<br>and<br>max.<br>freq.<br>(hz.) |
|-------|-------------------------------------|-------------------------------------|--|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|---|---------------------------------------|
| trens | -28.66                              | -23.46                              | -8.25                                  | 20.68                               | -24.07                              | -1.62                               | -1.314                              | -0.934                              | 917                                 | 0                                       | 32.6                                  |
| trens | 20.62                               | 25                                  | 49.3                                   | 25.55                               | 22.07                               | 1.092                               | 1                                   | 0.932                               | 0.919                               | 1430.3                                  | 567.5                                 |
| S.S.  | -4.558                              | -4.061                              | 8.976                                  | -3.031                              | -3.238                              | -0.994                              | -0.959                              | -0.924                              | -0.909                              | 1429.1                                  | 41                                    |
| S.S.  | 4.05                                | 4.606                               | 9.538                                  | 3.226                               | 3.227                               | 0.998                               | 0,963                               | 0.927                               | 0.912                               | 1429.5                                  | 46.7                                  |

Table 2 Performance of the motor during transient and steady state periods (with controller) T<sub>ref</sub> = 9.5 n.m. and N<sub>ref</sub> = 1410 r.p.m.

#### 5.3 Load torque disturbance

The performance of the motor is shown in Fig.5, the load torque is stepped down from its full load torque value to 0.8 full load. The minimum and maximum values of the currents, flux, torque, speed and frequency are given in Table 3.

|        | min.<br>and<br>max.<br>Ids<br>(amp. | min.<br>and<br>max.<br>Iqs<br>(amp.) | min.<br>end<br>mex.<br>torq.<br>(n.m.) | min.<br>and<br>max.<br>Idr<br>(amp. | min.<br>and<br>mex.<br>lqr<br>(amp. | min.<br>and<br>max.<br>¥ds<br>(wb.) | min.<br>and<br>max.<br>Yqs<br>(wb.) | min.<br>and<br>max.<br>Ydr<br>(wb.) | min.<br>and<br>max.<br>¥qr<br>(wb.) | min.<br>and<br>max.<br>Nr<br>(r.p.m. | min.<br>end<br>mex.<br>freq.<br>(hz.) |
|--------|-------------------------------------|--------------------------------------|--|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|--------------------------------------|---------------------------------------|
| trans. | -5.08                               | -5.145                               | 4.935                                  | -3.115                              | -3.264                              | -1.18                               | -1.188                              | -1.089                              | -1.088                              | 1425.6                               | 41.2                                  |
| trans. | 5.464                               | 5.196                                | 9.47                                   | -3.27                               | 3.027                               | 1,174                               | 1.194                               | 1.089                               | 1.09                                | 1465                                 | 81,2                                  |
| S.S.   | -4.288                              | -4.13                                | 6.087                                  | -2.373                              | -2.464                              | -1.16                               | -1.166                              | -1.089                              | -1.088                              | 1449.7                               | 47.7                                  |
| S.S.   | 4.639                               | 4.471                                | 8.248                                  | 2.379                               | 2.243                               | 1.172                               | 1.181                               | 1.083                               | 1.084                               | 1457.1                               | 73.2                                  |

Table 3 Performance of the motor during transient and steady state periods (with controller), T<sub>ref</sub>=9.5 n.m. and N<sub>ref</sub> = 1410 r.p.m., load torque is stepped down by 20% of full load torque

### 5.4 Load torque disturbance and step change in torque reference

Figure 6 shows the performance of the motor if the load torque is suddenly stepped down by 20% from its full load value and also the torque reference is stepped down from 9.5 n.m. to 7.6 n.m. The minimum and maximum values of the currents, flux, torque, speed and frequency are given in Table 4.

|      | min.<br>and<br>mex.<br>lds<br>(amp. | min.<br>and<br>max.<br>Iqs<br>(amp. | min.<br>and<br>mex.<br>torq.<br>(n.m.) | min.<br>and<br>max.<br>Idr<br>(amp. | min.<br>and<br>max.<br>Iqr<br>(amp. | min.<br>and<br>max.<br>¥ds<br>(wb.) | min.<br>and<br>max.<br>¥qs<br>(wb.) | min.<br>and<br>max.<br>Ydr<br>(wb.) | min.<br>and<br>max.<br>¥qr<br>(wb.) | inin.<br>and<br>rnax.<br>Nr<br>(r.p.m. | min.<br>and<br>max.<br>freq.<br>(hz.) |
|------|-------------------------------------|-------------------------------------|--|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|--|---------------------------------------|
| tren | -4.722                              | -4.61                               | 6.928                                  | -3.25                               | -3.302                              | 0.991                               | -1.04                               | -0.911                              | -0.907                              | 1425.6                                 | 35.55                                 |
| tran | 4.828                               | 4.617                               | 9.018                                  | 3.28                                | 3.227                               | 1.016                               | 0.99                                | 0.931                               | 0.926                               | 1439.                                  | 47.4                                  |
| S.S. | -3.934                              | -3.961                              | 7.186                                  | -2.926                              | -2.763                              | -9.35                               | -0.938                              | -0.879                              | -0.874                              | 1435.6                                 | 37.98                                 |
| S.S. | 3.943                               | 3.981                               | 7.703                                  | 2.874                               | 2.738                               | 0.898                               | 0.948                               | 0.888                               | 0.874                               | 1436.5                                 |                                       |

Table 4 Performance of the motor during transient and steady state periods (with controller),  $T_{ref}$  is stepped down from 9.5 n.m. to 7.4 n.m.,  $N_{ref} = 1410$  r.p.m. and load torque is stepped down by 20% full load torque.

#### 5.5 step change in speed reference

Figure 7 shows the performance of the motor when the stepped down the speed reference by 20% (from  $N_{ref}$ =1410 r.p.m. to  $N_{ref}$ = 1126 r.p.m.) at the torque reference = 9.5 n.m. Table 5 shows the minimum and maximum values of currents, flux, torque, speed and frequency during the steady state and transient periods.

|              | min.<br>and<br>max.<br>-Ids<br>(amp. | min.<br>and<br>max.<br>Iqs<br>(emp. | min.<br>and<br>max.<br>torq.<br>(n.m.) | min.<br>and<br>max.<br>Idr<br>(emp. | min.<br>and<br>max.<br>Iqr<br>(amp. | min.<br>and<br>max.<br>Yds<br>(wb.) | min.<br>and<br>max.<br>¥qs<br>(wb.) | min.<br>and<br>max.<br>Ydr<br>(wb.) | min.<br>and<br>max.<br>Yqr<br>(wb.) | min.<br>and<br>mex.<br>Nr<br>(r.p.m.) | min.<br>and<br>max.<br>freq.<br>(hz.) |
|--------------|--------------------------------------|-------------------------------------|--|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|---------------------------------------|---------------------------------------|
| trans        | -7.648                               | -7.893                              | 0.831                                  | -7.118                              | -7.212                              | -0.657                              | -0.007                              | -0.809                              | -0.695                              | 1170.6                                | 19.41                                 |
| trans        | 7.66                                 | 7.885                               | 9.364                                  | 7.117                               | 7.222                               | 1.016                               | 0.835                               | 0.931                               | 0.895                               | 1425.6                                | 47.4                                  |
| S.S.         | -7.646                               | -7.877                              | 9.07                                   | -7.11                               | -7.21                               | -0.552                              | -0.557                              | -0.425                              | -0.425                              | 1170.6                                | 25.42                                 |
| <b>3.5</b> . | -7.65                                | 7.885                               | 9.364                                  | 7,104                               | 7.2                                 | 0.55                                | 0.558                               | 0.424                               | 0.425                               | 1171.2                                | 28.31                                 |

Table 5 Performance of the motor during transient and steady state periods (with controller),  $N_{ref}$  is stepped down from 1410 r.p.m. to 1126 r.p.m. and  $T_{ref} = 9.5$  n.m.

#### 5.6 Step change in torque reference

The performance of the motor is shown in Fig.8 when the torque reference is stepped up from 9.5 to 11.4 n.m. at speed reference = 1410 r.p.m. Table 6 shows the minimum and maximum values of currents, flux, torque, speed and frequency during the steady state and transient periods.

|       | min.<br>and<br>max.<br>Ids<br>(amp. | min.<br>and<br>max.<br>Iqs<br>(amp. | min.<br>and<br>mex.<br>torq.<br>(n.m.) | min.<br>and<br>max.<br>Idr<br>(amp. | min.<br>and<br>mex.<br>iqr<br>(amp. | min.<br>and<br>max.<br>乎ds<br>(wb.) | min.<br>and<br>mex.<br>¥qs<br>(wb.) | min.<br>and<br>mex.<br>¥dr<br>(wb.) | min.<br>and<br>mex.<br>Yqr<br>(wb.) | min.<br>and<br>max.<br>Nr<br>(r.p.m.) | min.<br>and<br>max.<br>freq.<br>(hz.) |
|-------|-------------------------------------|-------------------------------------|--|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|---------------------------------------|---------------------------------------|
| trans | -5.633                              | -5.549                              | 7.131                                  | -3.592                              | -3.765                              | -1.172                              | -1.176                              | -1.077                              | -1.079                              | 1425.6                                | 42.54                                 |
| trans | 5.687                               | 5.53                                | 11.31                                  | 3.835                               | 3.709                               | 1.161                               | 1.166                               | 1.081                               | 1.08                                | 1452.7                                | 80.84                                 |
| 5.8.  | -4.47                               | -4.63                               | 8.4                                    | -3.099                              | -2.93                               | -1.137                              | -1.147                              | -1.064                              | -1.063                              | 1445.4                                | 46.92                                 |
| S.S.  | 4.55                                | 4.579                               | 10.28                                  | 3.129                               | 2.999                               | 1.14                                | 1.145                               | 1.07                                | 1.067                               | 1449.8                                | 65.60                                 |

Table 6 Performace of the during transient and steady state periods (with controller), Tref is stepped up from 9.5 n.m. to 11.4 n.m. and N<sub>ref</sub>=1410 r.p.m.

Also, by controlling the reference speed or the reference torque, it is possible to control the performance of the motor. It can be noted that from the comparison between the starting-up of the motor without controller and with controller, the possibility to control the over shoot of the speed by controlling  $W_{\text{ref}}$  ( $W_{\text{ref}}$  = 2  $\pi$   $N_{\text{ref}}$ ), the fluctuating of speed during the steady state period and without using the controller is between 1447.6 and 1448.817 r.p.m. and it is between 1429.135 and

1429.54 r.p.m. with the controller and  $N_{\rm ref}=1410$  r.p.m. Also the fluctuating of torque during steady state period is between 8.123 and 10.31 n.m. without using controller and it is between 8.976 and 9.538 n.m. with using the controller and  $T_{\rm ref}=9.5$  n.m. If the disturbance in load torque has occurred, the performance of the motor is still with the acceptable limits.

#### 6. Conclusions

A proposed simplified algorithm has been provided. Performance of the motor during starting-up and steady-state periods have been studied. The results showed that the motor speed due to the disturbance in load torque is still with the acceptable limit.

#### 7. Reference

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#### List of symbols

 $\Psi_{ds}$ ,  $\Psi_{qs}$ : direct and quadrature axes stator flux linkage

 $\Psi_{dr}$ ,  $\Psi_{qr}$ : direct and quadrature axes rotor flux linkage

 $\alpha_i$ : ith switching angle (i = 1 ...... M)

E: Maximum value of output voltage of PVVM inverter.

F: frequency of input voltage of the motor

Fn: nominal frequency of the input voltage

 $\mathbf{I}_{ds}$  ,  $\mathbf{I}_{qs}$  : direct and quadrature axes components of stator current.

 $\mathbf{I}_{dr}$  ,  $\mathbf{I}_{qr}$  ; direct and quadrature axes components of rotor current.

 $i_a$  ,  $i_b$  ,  $i_C$  : currents of phases a, b and c resp.

J. K: moment of inertia and friction constant

 $K_{\rm S}$  ,  $K_{\rm T}$  : proportional gain constant of speed and torque PI controller

Ls, Lr: apparent three phase stator and rotor self-inductance

Lar: apparent three phase mutual-inductance

M: no of switching angles per quarter cycle

N<sub>ref</sub>: reference rotor speed in r.p.m.

P: no of pair poles

Rs , Rr: stator and rotor resistance

S : slip of the motor = (We-WR)/We

O: arbtrary electrical angular position

t: time in sec.

Te: electromagnetic torque

Tref : reference torque

Tes. Tr : time constant of of speed and torque PI controller

T<sub>i</sub>: load torque

Va, Vb, Vc: voltage of phases a, b and c

 $V_{dS}$ ,  $V_{dS}$ : direct-and-quadrature axes component of stator voltage

V<sub>dr</sub>, V<sub>dr</sub>: direct-and-quadrature axes component of rotor voltage

 $V_r: r\underline{th}$  harmonic of the input voltage wave form of PWM inverter

Vn : nominal amplitude of the motor input voltage

Wa : arbitrary electrical angular velocity

 $W_{\rm eq}$ : electrical angular velocity = 2  $\pi$  F

W<sub>m</sub>: rotor angular velocity

 $W_{ref}$ : reference angular velocity = 2  $\pi$  N<sub>ref</sub> /60

WR : electrical angular rotor speed

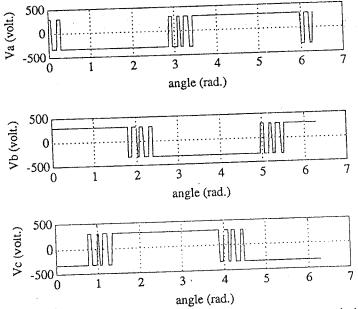


Fig.(1) optimum PWM inverter voltage in phase a,phase b and phase c

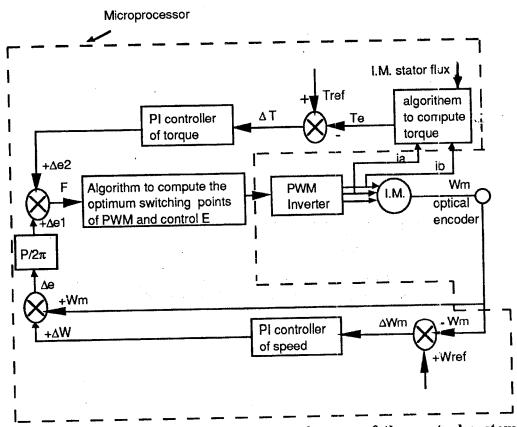


Fig.(2) Basic schematic diagram of the control system

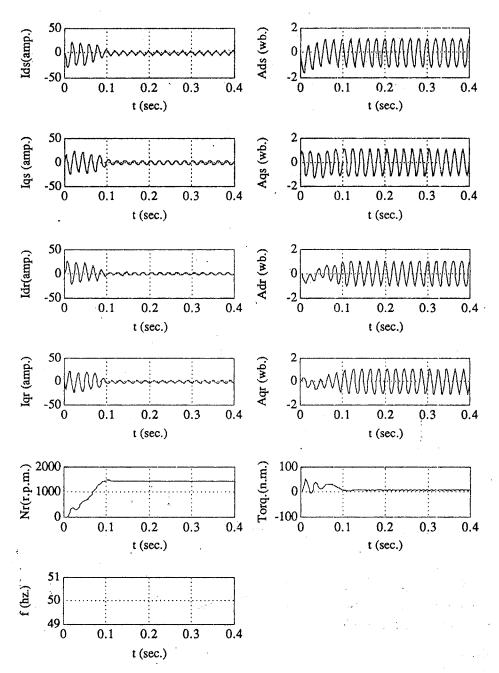


Fig.(3) The performance of the motor during starting period and steady state period without controller and fed by optimum PWM inverter

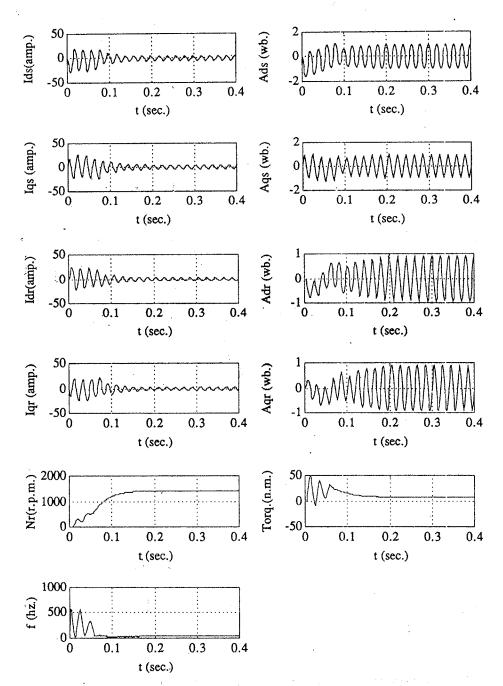


Fig.(4) The performance of the motor during starting period and steady state period with controller and fed by optimum PWM inverter (Tref.=9.5 n.m. & Nref = 1410 r.p.m.)

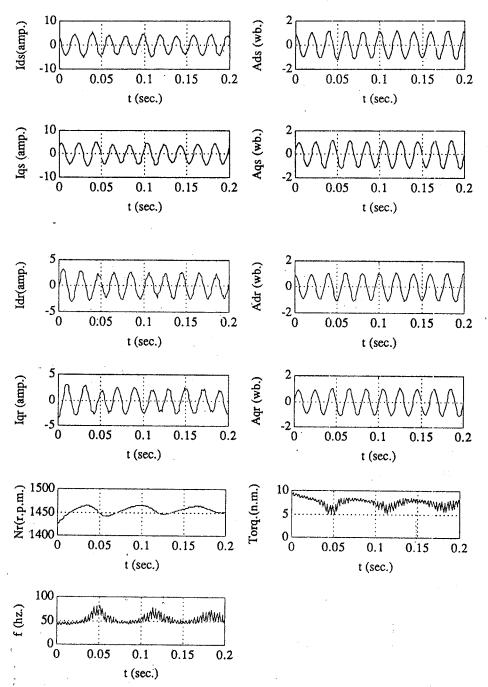


Fig.(5) The performance of the motor during step down of load torque by 20% full load torque and Tref. = 9.5 n.m. & Nref = 1410 r.p.m.

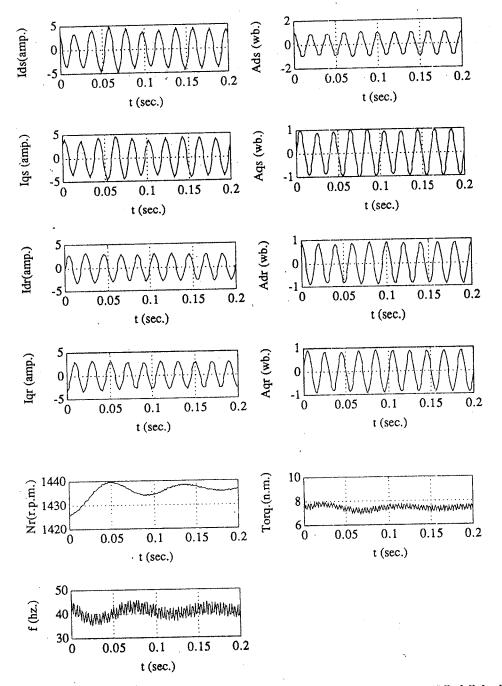


Fig.(6) The performance of the motor during step down of load torque by 20% full load torque and Tref. is stepped down from 9.5 n.m. ---> 7.4 n.m. & Nref = 1410 r.p.m.

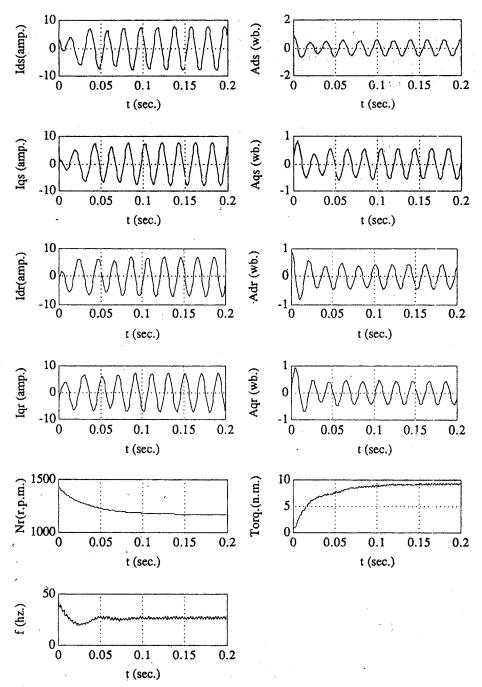


Fig.(7) The performance of the motor during step down of Nref by 20% rated value (Tref.=9.5 n.m. & Nref = 1410 r.p.m. ----> 1126 r.p.m.)

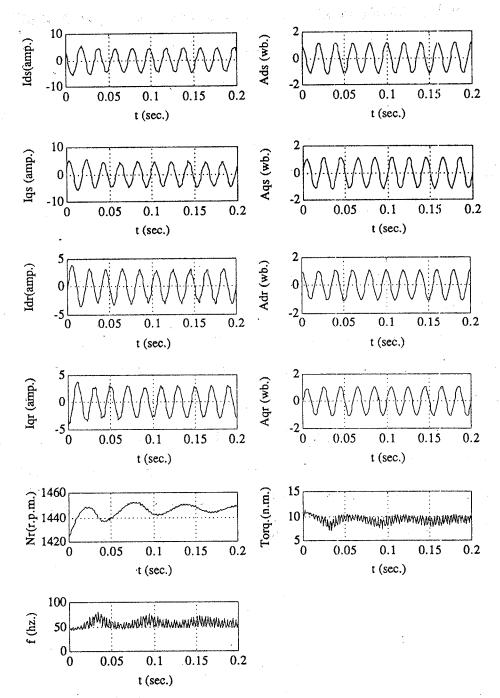


Fig.(8) The performance of the motor during step up of Tref by 20% rated value ( Tref. > 9.5 n.m. ---> 11.4 n.m. & Nref = 1410 r.p.m.)

# التحكم الرقمى في سرعة محرك حثى ثلاثى الوجه بإستخدام التعديل النبضى الأمثل للحصول على تيار متغير

## الملخص

في الآونة الأخيرة ظهرت تطبيقات عديدة بإستخدام أساليب الميكروبروسيسور في مجال التحكم في المحركات ذات السرعات المتغيرة مثل المحرك الحثى ثلاثى الأوجه،

ويتناول هذا البحث طريقة مبتكرة للتحكم المحكم في سرعة محرك حتى ثلاثم الأوجمه المغذى بجهد متغير المتردد ونلك بإستخدام الميكروبروسيسور والطريقة المقترحة في التحكم تعتمد على أساس بناء الجوريثم مبسط يقوم بحساب لحظات التوصيل لمقطع الجهد بإستخدام التعديل النبضي الأمثل للحصول على تيار متغير بحتوى على أقل عدد ممكن من التوافقيات وبالتالي التحكم في تردد الجهد المتغير المغذى للمحرك تحت شرط ثبوت الفولت/التردد أثناء التشغيل، وتشتمل البحث على دراسة لأداء المحرك خلال الفترات الإنتقالية والإستقرار عند حدوث تغير مفاجئ في الحمل و أيضا عند حدوث تغير ولمقارن والمقارن والمقارن المقارن والمقارن المقارن الم