

# Modeling and Simulation of the Shape Error in the ECM Process

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**Abstract:** Accuracy in ECM is still a problem that restricts the application of this technology for accurate applications. The present investigation submits a theoretical and experimental study about shape error in the ECM process which has not been attempted before. Feed rate, applied voltage, electrolyte conductivity and initial gap size have been considered the main factors affecting the shape error value (sometimes reached 40  $\mu\text{m}$  for a 40 mm workpiece length). Experimental results have been found to agree with the estimated values with a difference less than 0.01 mm. The present results emphasize the importance of the consideration of the shape error factor for accurate tool design and shape prediction

## 1. Introduction

Metal removal in the ECM process takes place when a voltage is applied between two metal electrodes that are immersed in an electrolyte. "Ions," electrically charged groups of atoms, migrate physically through the electrolyte and in doing so carry the current. The transfer of electrons between the ions and electrodes completes the electrical circuit which allows the workpiece to be dissolved.[1-2].

The process was developed primarily to machine advanced aerospace materials for complex shapes. Currently, ECM is used in areas such as aerospace, automotive, nuclear, surgical implant components, computer parts, forging dies, etc., for fast production with high quality surface and burr free [3].

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The accuracy of the ECM process should be considered from several views: compliance of the finished part with its drawing in terms of shape and dimensions; transfer of tool shape to the workpiece; and repeatability dimensions in parts taken from a sufficiently large lot machined with the same electrode tool. In electrochemical die sinking the primary objective is to maintain the form tolerance as closely as practicable. To achieve this, it is essential to use a tool of the right form and size and the right process parameters. This requires the design of a suitable tool and, in consequence, the computation of the form and dimensions of the finished part that will be produced by a given tool. All of this can be done only from an analysis of ECM accuracy, in other words, it is important to know how machining accuracy is affected by differences in the actual profile of the tool from the design one and in the process parameters from those for which the tool has been designed [4].

An accurate design of the electrode tool in many cases cannot be done for lack of knowledge about some quantitative aspects of the events occurring in the ECM process and due to mathematical difficulties in solving field problems [3]. It is usual practice, therefore, to build an approximate, but sufficiently adequate model of the object, to find a solution for the model, and to refine the solution and model as may be necessary [4]. More specifically, one selects few key factors to describe their effect on the forming process and finally apply whatever corrections may be necessary in order to account for the influences left out of consideration.

Many papers concerning the accuracy in the ECM process have been published [5-8]. Most of these publications have been presented to model and simulate the geometry of the gap size in the ECM process [9-13]. However, hardly, no publications have been submitted about the general models for the shape error of the workpiece profile in the ECM process. Shape error represents the difference between the maximum and minimum dimension of the workpiece profile after ECM action (Fig. 1). Certainly, this factor could affect the ECM accuracy.

The objectives of this investigation are: 1) develop the theoretical models for the shape error of the workpiece profile in the ECM process; 2) perform computer simulation concerning the shape error of the workpiece; 3) analyze the influence of the process parameters occurring within the machining area on shape error of the workpiece profile; 4) design and carry out the experiments to verify the developed theoretical models.

## 2 Theoretical Models of Shape Error in ECM

Shape error is the difference between the maximum and minimum dimension of the workpiece profile after the ECM process. Shape error is affected by the non-steady physical phenomena in the gap, such as conjugate fields of the electrolyte flow velocity, static pressures, temperature, gas concentrations, current densities, and metal removal rate distribution on the workpiece surface [4]. The Theoretical models and the analyses based on the models not only give a deeper insight into the ECM gap and anodic processes, but also lay a foundation for the development of the process simulation, computer-aided shape prediction, and tool design [9].

To develop a theoretical model for shape error in ECM, the following assumptions have been made: (a) Ohm's law holds over the entire gap up to the surface of the electrodes; (b) at each electrode, the potential remains the same over the entire surface area and through out the machining time; (c) the angle between feed rate and dissolution  $\alpha$  is neglected (Fig. 2); (d) heat transfer through the electrolyte is neglected; (e) the volumetric electrochemical equivalent  $K_v$  remains constant in both time and space; (f) the pressure in the interelectrode gap is assumed to be linearly decreasing and dropping to atmospheric pressure at the outlet.

Based on the previous assumptions, the theoretical model of shape error in the ECM process with constant feed rate in the steady state will be defined first. The effect of temperature rise and hydrogen gas bubble on the gap value will be achieved.

### 2.1 Shape Error Definition

The shape error  $\Delta B$  is defined as the difference between the maximum and the minimum dimensions of the workpiece profile after ECM action which is equal to the difference between  $S_{\max}$  and  $S_{\min}$  ( Fig. 1 )

$$\Delta B = S_{\max} - S_{\min} \quad (1)$$

where  $S_{\max}$  and  $S_{\min}$  are maximum and minimum gap size respectively. The gap sizes equation can be written in the form of :

$$S(x) = S_f^0 (1 + \alpha_T \theta) (1 - \beta)^{\frac{3}{2}} \quad (2)$$

where:

$\alpha_T$  is temperature coefficient of electrolyte conductivity (1/K),

$\theta$  is temperature increment of the electrolyte in the gap (degree, K),

$\beta$  is the volume concentration of gas in the gap,

$S_f^0$  is the inlet gap size in the steady state. The conductivity can be derived by combining Bruggeman's relation [14]

$$\chi = \chi_0(1 + \alpha_T \theta)(1 - \beta)^{\frac{3}{2}} \quad (3)$$

where :

$\chi_0$  is the inlet electrolyte conductivity (A/v.mm )

According to Ohm's Law, the current density can be estimated as follows:

$$i = \chi_0(1 + \alpha_T \theta)(1 - \beta)^{\frac{3}{2}} \cdot \frac{U_0 - \Delta U}{S} \quad (4)$$

where:

$U_0$  is the voltage (volt), and  $\Delta U$  is over potential (volt).

$$\theta = T - T_0 \quad (5)$$

In order to evaluate the maximum and minimum gap size, the temperature and the concentration of gas should be calculated as following

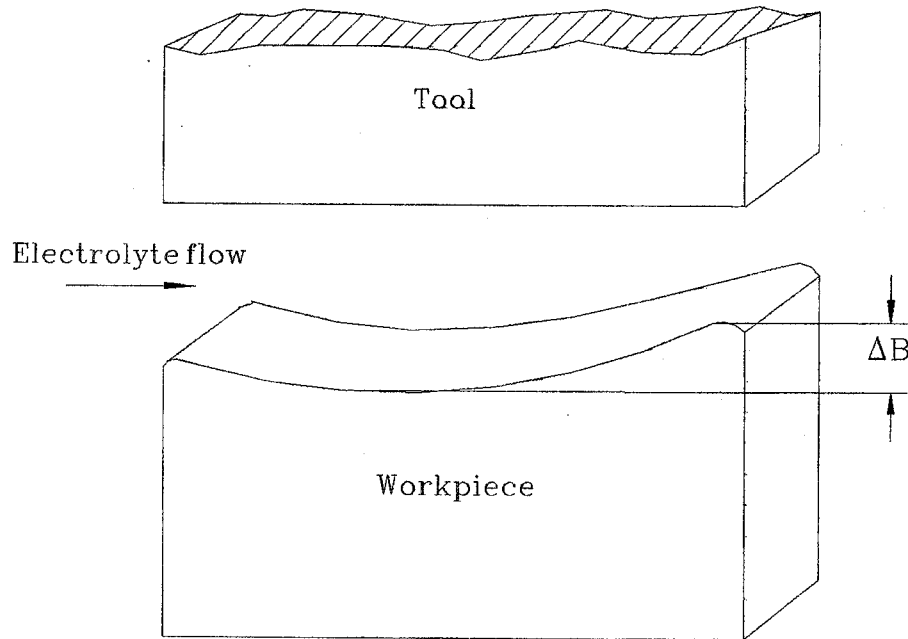


Fig. 1 . Shape error in the ECM process

## 2.2 Temperature in the Gap

The increment of temperature in the gap has been derived as follows [10]

$$\theta = \frac{U_0 \frac{V_f}{K_v}}{\rho_0 S_0 w_0 C} X \quad (6)$$

where :

$V_f$  is the tool feed rate (mm/min),  
 $K_v$  is the volumetric electrochemical equivalent of the anodic material (mm<sup>3</sup>/A.min),

$\rho_0$  is the density of electrolyte medium (kg/mm<sup>3</sup>),

$w_0$  is the inlet velocity of electrolyte (m/sec),

$S_0$  is the initial gap size (mm), and

$C$  is the heat conductivity (J/kg.degree),

$X$  is the distance from inlet (mm) (Fig 2).

The flow rate is

$$Q_v = S_0 w_0 b \quad (7)$$

where

$B$  is width of the workpiece. Considering  $X = G$ , where  $G$  is the whole length of workpiece, the maximum increment of temperature can then be expressed as

$$\theta_{\max} = \frac{U_0 V_f b G}{\rho_0 K_v C Q_v} \quad (8)$$

Substituting Eq. (6) into Eq.(5), yields

$$T = T_0 + \frac{U_0 i X}{w_0 S_0 \rho_0 C} \quad (9)$$

where

$i$  is the current density (A/mm<sup>2</sup>)

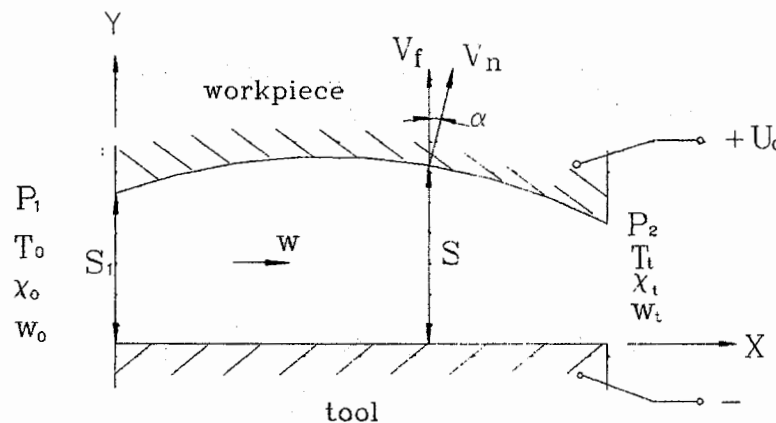


Fig. 2 . Schematic diagram showing the relation between feed rate and normal direction of anode

### 2.3 Volumetric Concentration of Gas

It is clear from Eq. (4), that the gas content affects the current density, and consequently it affects the material removal rate. Analysis of gas content in the gap is very important for the calculation of shape error.

Figure 3 shows how electrolyte temperature and gas content affect the distribution of local metal-removal rates in a plane-parallel gap. The hydrogen evolving at the tool produces a two-phase layer (electrolyte and hydrogen bubbles). Under certain conditions, this layer may fill all of the gap.

The next equation focuses on the calculation of the volumetric concentration of gas which represents the effect of hydrogen on the electrolyte conductivity (Eq. 3). The volumetric concentration of gas is defined as

$$\beta = \frac{V_{gas}}{V_{total}} \quad (10)$$

where :

$V_{gas}$  is the volume of gas

$V_{total}$  is the total volume.

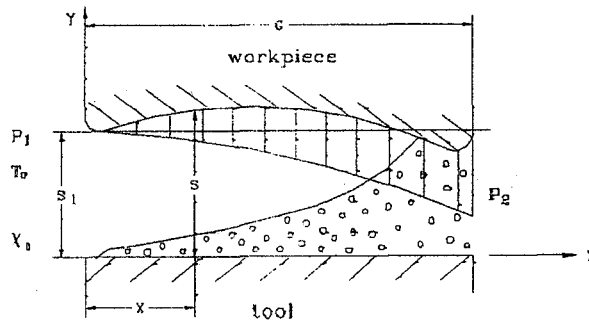


Fig. 3 . Distribution of gas bubbles along the ECM gap  
After Rumyantsev and Davydov [4]

Total mass in the gap is

$$m_t = \rho_g \beta V_{total} + (V_{total} - V_{gas}) \rho_e \quad (11)$$

where :

$m_t$  is the total mass in the gap,

$\rho_g$  is the density of gas and

$\rho_e$  is the density of electrolyte.

The density of the electrolyte medium can be expressed as [4]

$$\rho_m = \frac{m_m}{V_{total}} \quad (12)$$

where :

$\rho_m$  is density of the medium,

$m_m$  is the mass of medium and

$V_{total}$  is the total volume of medium.

It can also be written in the form of

$$\rho_m = \rho_g \beta + (1 - \beta) \rho_e \quad (13)$$

where :

$\rho_g$  is the density of gas,

$\rho_e$  is the density of electrolyte and

$\beta$  is the concentration of gas.

Since  $\rho_g \beta$  is much less than  $(1 - \beta) \rho_e$ , one will have

$$\rho_m \cong (1 - \beta) \rho_e \quad (14)$$

The mass of the electrolyte medium is conservative, i.e.,

$$\rho_0 w_0 S_0 = \rho_m w S \quad (15)$$

where

$\rho_0$  is the density of the medium at the inlet. Since  $\rho_e = \rho_0$ , then

$$\rho_0 w_0 S_0 = \rho_0 (1 - \beta) w S \quad (16)$$

The flow velocity can be written as

$$w = \frac{w_0 S_0}{S(1 - \beta)} \quad (17)$$

By using the pressure relation [16] yields

$$P_1 - P_2 = \lambda \cdot \frac{G}{2S} \cdot \rho \cdot \frac{\bar{w}^2}{2} \quad (18)$$

By using Blasious formula [16]:

where :

for turbulent flow

$$n = 0.316$$

$$m = 0.25$$

for laminar flow

$$n=96,$$

$$m=1,$$

$R_e$  is Reynolds number, and viscosity ( $\gamma = \frac{\mu}{\rho}$  m<sup>2</sup>/sec).

$W$  is the main electrolyte velocity

For turbulent flow, flow velocity can be expressed as

$$w_0 = \left[ \frac{S_f \left( \frac{2S_f}{\gamma} \right)^{0.25} \Delta P}{0.0079G\rho} \right]^{1.75} \quad (19)$$

where

$\Delta P = P_1 - P_2$  is the pressure difference (MPa), ; for laminar flow, the flow velocity can be expressed as

$$w_0 = \frac{S_f^2 \Delta P}{12G\rho\gamma} \quad (20)$$

where

$S_f$  is the stationary gap size

According to Faraday's Law, the mass of electrolyte medium is

$$m = KIt \quad (21)$$

where

$K$  is the current efficiency,

$I$  is current (A) and

$t$  is time (sec).

Referring Eq.(21) the mass volume of the gas  $m_{H2}$  can be written as

$$m_{H2} = K_{H2} i b \cdot dx \cdot dt \quad (22)$$

where

$b$  is the width of the gap (mm),

$i$  is the current density (A/mm<sup>2</sup>).

Therefore, the mass of the gas is

$$m_{H2} = K_{H2} b \int_0^x i \cdot dx \cdot dt \quad (23)$$

i.e.,

$$m_{H2} = K_{H2} b i X dt \quad (24)$$

The mass of gas can also be presented as



$$m_{H_2} = \rho_{H_2} \beta w S b d t, \quad (25)$$

where

$S$  is the gap size, Equating Eq.(24) and Eq.(25), we get

$$K_{H_2} i X = \rho_{H_2} \beta w S \quad (26)$$

Substituting Eq.(18) into Eq.(26), we get

$$\beta = \frac{K_{vH_2} \cdot \frac{iX}{w_0 S_0}}{1 + K_{vH_2} \cdot \frac{iX}{w_0 S_0}}, \quad (27)$$

where :

$K_{vH_2}$  is the volume of the hydrogen generated per ampere of current per second of time ( $m^3/A \cdot sec$ ), it can be defined as

$$K_{vH_2} = \frac{K_{H_2}}{\rho_{H_2}},$$

where

$K_{H_2}$  is the coefficient of gas,

$\rho_{H_2}$  is density of gas.

For perfect gas by referring to Acharya et al. [17], we have

$$PV = \frac{m_{H_2}}{\mu} R_{\mu} T, \quad (28)$$

where

$P$  is the pressure

$$P(x) = P_1 - \frac{P_1 - P_2}{G} X, \quad (29)$$

where

$V$  is the volume,

$T$  is the temperature,

$m_{H_2}$  is the mass of gas in the volume,

$R_{\mu}$  is the gas constant and

$\mu$  is the weight of atom mass. Eq.(27) can also be written as

$$\frac{P}{\rho_g} = \frac{R_{\mu}}{\mu} T \quad (30)$$

$$\frac{P_n}{\rho_n} = \frac{R_{\mu}}{\mu} T_n \quad (31)$$

where

$$\rho_g = \frac{m}{V},$$

$P_n$  is the normal pressure,

$T_n$  is the normal temperature.

Dividing Eq.(31) by Eq.(29), yields

$$\rho_g = \rho_n \frac{PT_n}{P_n T} \quad (32)$$

Multiplying Eq.(32) by  $K_{H2}$  on both sides, comes out

$$K_{vH2} = \frac{K_{H2}}{\rho_n} \cdot \frac{P_n}{P} \cdot \frac{T}{T_n} \quad (33)$$

Substituting Eq.(33) into Eq.(27), yields

$$\beta = \frac{\frac{K_{H2}}{\rho_n} \cdot \frac{P_n}{P} \cdot \frac{T}{T_n} \cdot \frac{iX}{w_0 S_0}}{1 + \frac{K_{H2}}{\rho_n} \cdot \frac{P_n}{P} \cdot \frac{T}{T_n} \cdot \frac{iX}{w_0 S_0}}, \quad (34)$$

where

$$i = \frac{V_f}{K_v} \cdot \frac{K_{H2}}{\rho_n} = 1.25 \times 10^{-7} (m^3/A \cdot sec)$$

$$P_n = 10^5 (N/m^2) \text{ and}$$

$$T_n = 273^\circ k$$

Eq.(33) can then be written as

$$K_{vH2} = \varepsilon_H 1.25 \times 10^{-7} \cdot \frac{10^5}{P} \cdot \frac{T}{273} \quad (35)$$

where

$\varepsilon_H$  is the efficiency of gas,

$\varepsilon_H = 1$  for NaCl,

$\varepsilon_H = 0.6$  for NaNO<sub>3</sub> [10].

### 3. Computer Simulation of the Shape Error

In order to analyze the shape error of the workpiece in the ECM process and to predict it, the computer simulation has been performed by using the theoretical models developed in the previous section. The parameters used in the simulation of the shape error are collected from experimental results and listed in Table 1 for stationary and feed rate cases.

Table 1 The parameters used in the simulation of the shape error

No	Parameter	Symbol	Value	Unit	Comments
1	Over potential	$\Delta U$	2	volt	Ref.[8]
2	Density of electrolyte	$\rho$	1120	kg / m <sup>3</sup>	Experimental
3	Viscosity of electrolyte	$\gamma$	10 <sup>-6</sup>	m <sup>2</sup> / sec	Ref.[11]
4	Electrolyte conductivity in the inlet	$\chi_0$	0.0117	A/v.mm	Experimental
5	Volumetric electrochemical equivalent	$K_v$	1.9	mm <sup>3</sup> / A · min	Experimental
6	Inlet temperature	$T_0$	293 k (20°C)	degree	Ref.[11]
7	Critical Reynolds number	$R_c$	2400		Ref.[16]
8	Heat conductivity of electrolyte	$C$	3700	J / kg · deg	Ref.[11]
9	Temperature coefficient	$\alpha_T$	0.02	1/deg.	Ref.[11]

### 4. Experimental Verification

The experiments were performed on an ECM cell, which consists of an electrolyte holding tank, a pump, power supply and appropriate hosing and pressure fittings to transport the electrolyte to and from the electrochemical cell (Fig. 4). Measurements have been used to conduct the electrochemical accuracy experiments included an IBM compatible 386/25 MHz PC, conductivity and temperature probe meters (Orion, model 160), a precision laboratory scale (Sartorius, E-1200S) with a readability of 0.1mg, and a state-of-the-art high speed data acquisition package (ISO-16) to collect data from the ECM cell. A

Brown & Sharp Microval Coordinate Measuring Machine (CMM) was used to measure the dimensions of workpiece after and before the ECM process.

The constructed ECM machining cell, consists of a cathode (tool) and an anode (workpiece) kept at a constant gap from each other by controlling the height of the tool with an accuracy of 0.01mm through CMM equipment. The cell was designed to withstand a high electrolyte pressure. The constructed cell was made from stainless steel 304 and Teflon to avoid the corrosion and to reduce the tool and the workpiece fixture wear. Tool and workpiece holders were made from 304 stainless steel. The machined specimen is of a rectangular shape ( height  $A=22.86$  mm, width  $b=3.073$  mm, length  $G=40$ mm and surface area of  $122.8$  mm<sup>2</sup>). The specimens were made of ground die steel (Badger 01) produced in U.S.A.(0.94% Carbon, 0.3% Silicon, 1.2% Manganese, 0.5% Tungsten, 0.5% Chromium). The electrolytes used in these experiments were 15% NaNO<sub>3</sub> and 15% NaCl aqueous solutions (by weight) maintained at initial temperature of 20° C. To overcome the problem of temperature rise during the ECM process a large quantity of electrolyte was pumped through the working gap to minimize the temperature rise. The experiments have been done under stationary tool feed rate conditions.

The experimental set-up includes a precision engineered transistorized power supply. The generator is capable of supplying maximum currents of 200 amperes, a voltage ranging from 5 to 30 volts with 0.5% RMS. ripple. This is controlled by a Siemens power relay which in turn is controlled by a Gralab 645 Digital timer for accurate machining time and easy control. Accurate machining timer was needed for calculating the material removal rates precisely.

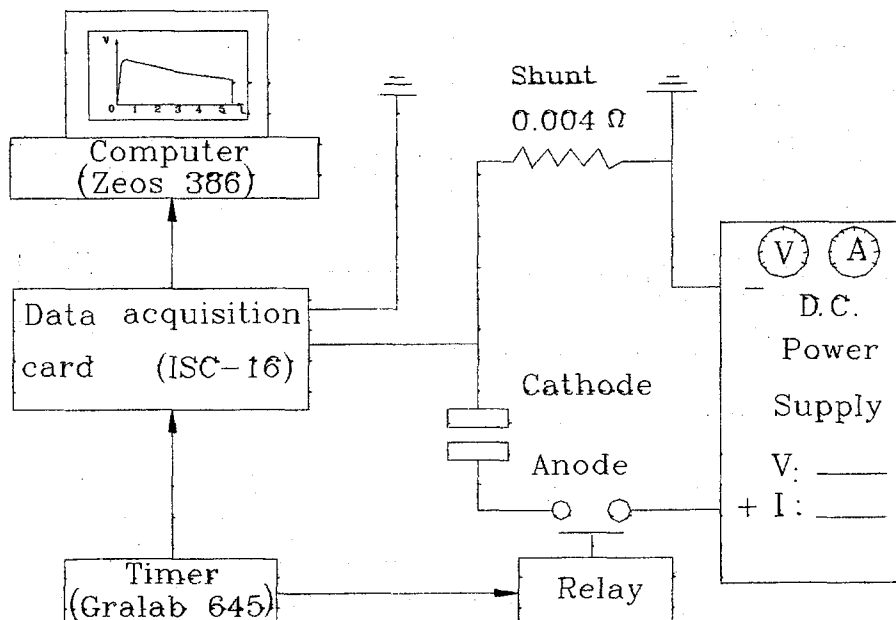


Fig. 4 Schematic diagram of the data acquisition system for the ECM cell.

Electrolyte temperature, inlet pressure, electrolyte flow rate and gas content are the main factors which affect the distribution of local metal-removal rates in a plane-parallel gap. The present results have been collected from 228 measurements carried out on the stationary conditions. Experimental results are shown in Figs. 5-9 as dashed lines. Each point comes from 3 experiments and each point has been measured 4 times and then the average was computed. The solid lines are the calculations of the mathematical models. It is shown that the calculation of the results are quite promising with the experimental results. The theoretical models can, therefore, be used to simulate and predict the shape error.

Figures. 5-6 show that shape error  $\Delta B$  decreases as the machining time ( $t$ ) increases, for NaCl (Fig. 5), and NaNO<sub>3</sub> (Fig. 6) electrolyte. This result has been attributed to the decrease of the metal removal rate at the wide gap values which consequently decreases the variation difference in the resultant metal removal. Figure 7 shows that as voltage increases  $\Delta B$  increases. This result is due to the increase of the variation of the metal removal rate at the high current density values. Figure 8 shows that as initial gap length increases  $\Delta B$  decreases because of the decrease of the metal removal rate. Figure 9 shows the limited effect of the electrolyte pressure on the decrease of the shape error value. Figs.10 -13 show the shape profile of the workpiece after machining under different machining times. Shape profile has been drawn through 10 points, each point has been measured 5 times and then computed the average. It is seen that the effect of the increase of temperature leads to increase of the metal removal during all the first half portion from the inlet. However, after certain machining time, the effect of gas concentration became pronounced and led to less metal removal as the flow progress. This is the reason for the concavity of the workpiece profile. For 57 experiments have been conducted the maximum shape error in the present work was 36  $\mu\text{m}$ . The maximum variation between theoretical and experimental results was about 10  $\mu\text{m}$  which consequently emphasizes the analysis and the computer simulation.

## 5. Conclusions

- Experimental results proved that shape error is a vital factor in the accuracy of the ECM process. It should be considered during the analysis of the ECM accuracy ( $\Delta B$  is about 0.04 mm along 40 mm workpiece length).
- Theoretical analysis and experimental results were confined with each other with a variation usually less than 0.01 mm, which emphasizes the adequacy of the suggested model.
- The shape error factor could be extended for further applications with complex shapes as an endeavour towards the enhancement of the ECM accuracy.

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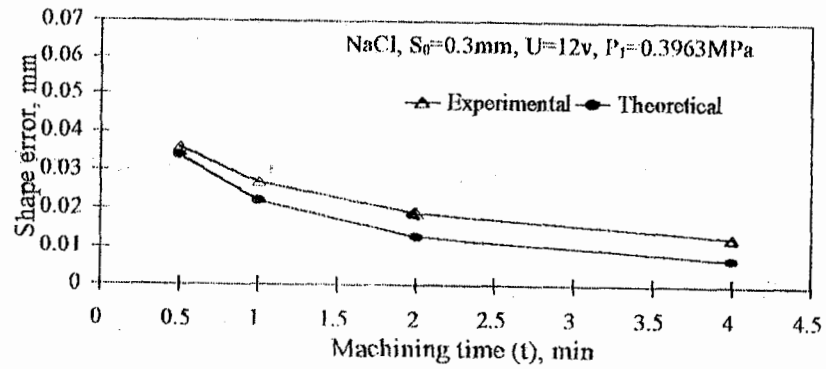


Fig. 5 Effect of machining time on shape error with NaCl

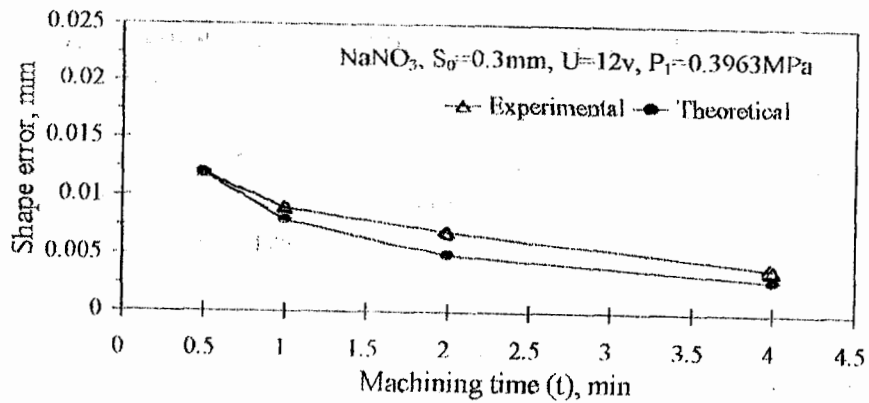


Fig. 6 Effect of machining time on shape error with  $\text{NaNO}_3$

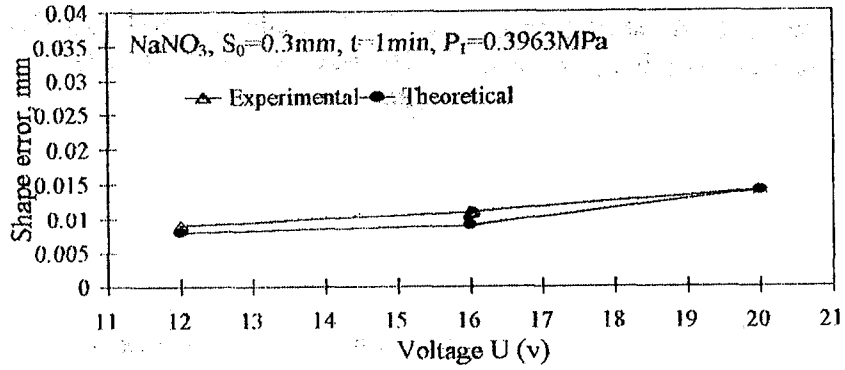


Fig. 7 Effect of the applied voltage on shape error

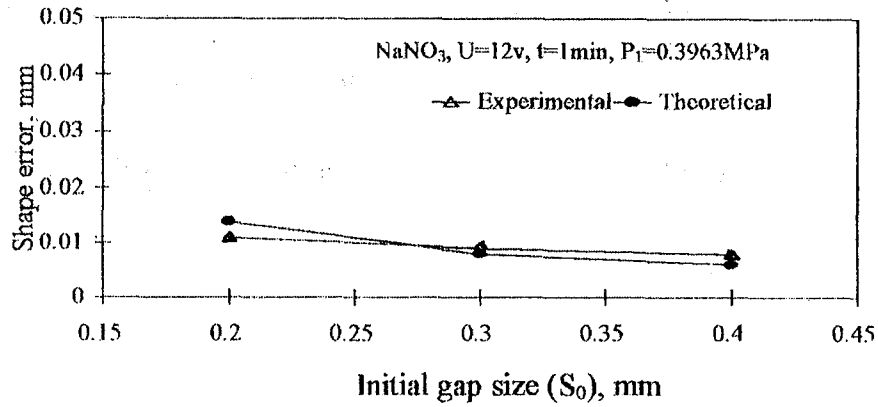


Fig. 8 Effect of the initial gap size on shape error

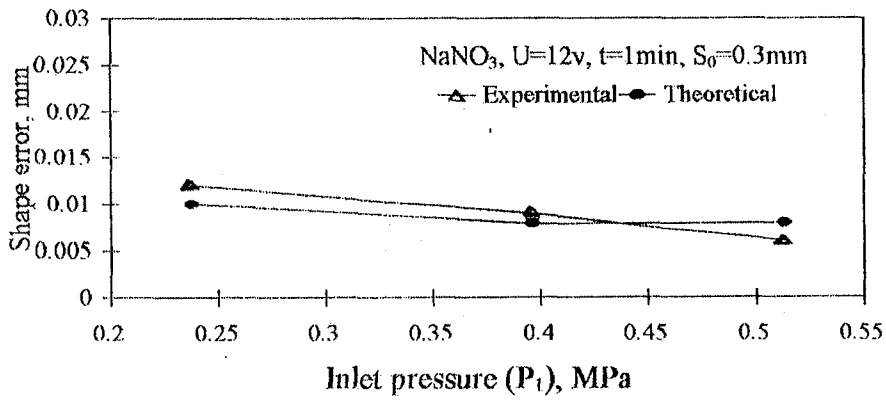


Fig. 9 Effect of the inlet pressure on shape error



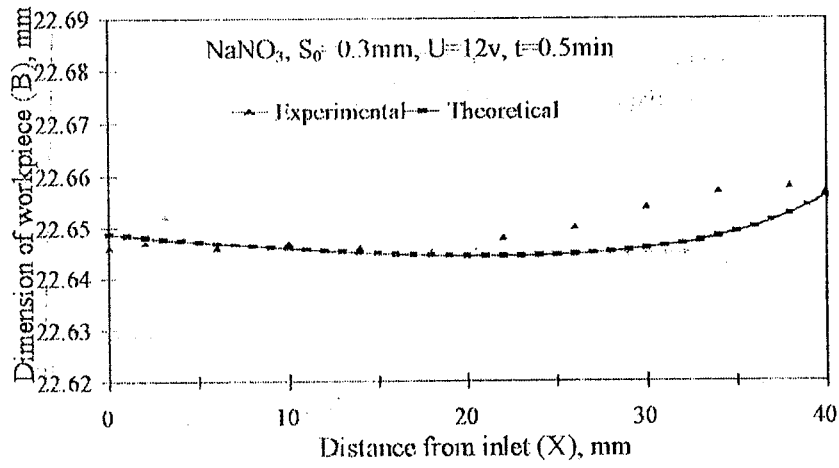


Fig. 10 Shape of workpiece after machining

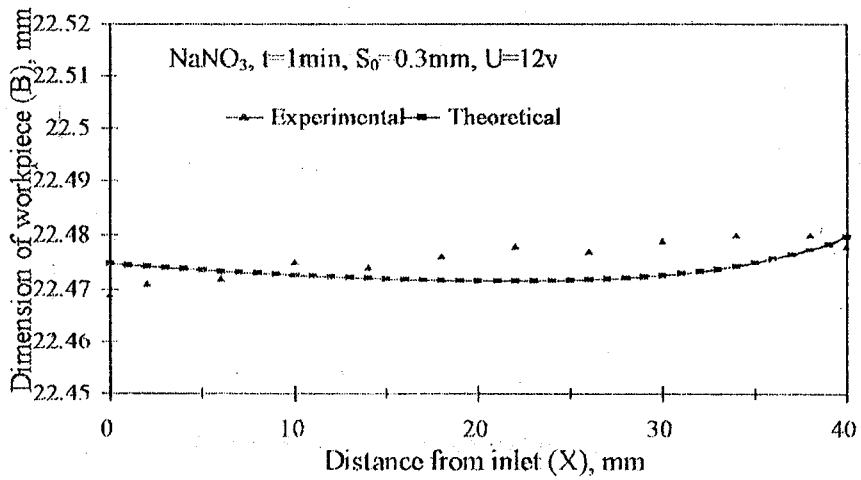


Fig. 11 Shape of workpiece after machining

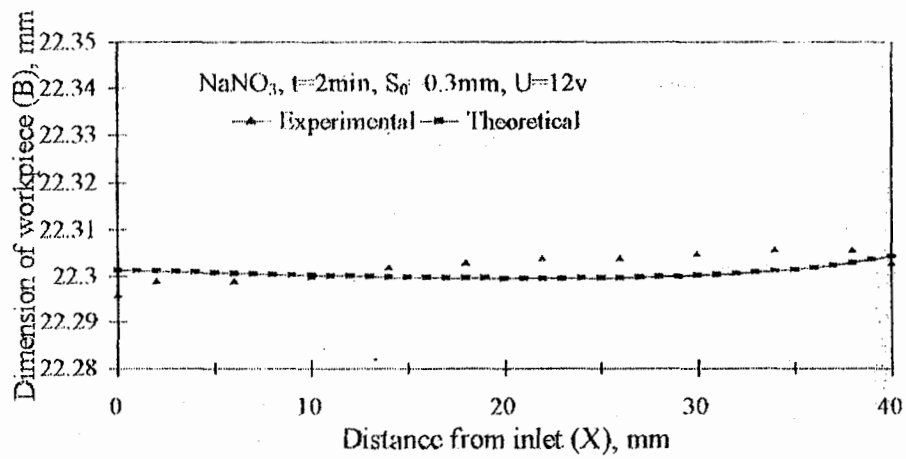


Fig. 12 Shape of workpiece after machining

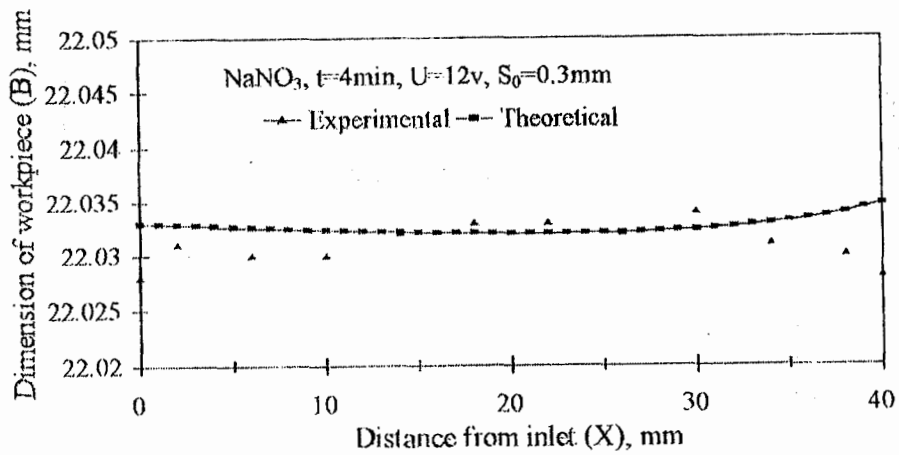


Fig. 13 Shape of workpiece after machining

## النمذجة والمحاكاة للخطأ الشكلي في عمليات التشغيل الكهروكيميائي

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## المخلص

يتناول البحث جانبا من جوانب الدقة لعمليات التشغيل الكهروكيميائي والمسمى بالخطأ الشكلي او الانحراف فى الشكل وهو عبارة عن الفارق بين اكبر ارتفاع واقل انخفاض فى ابعاد المنتج النهائية عقب انتهاء عملية التشغيل الكهرو كيميائي .والبحث دراسة عملية ونظرية احتوت كثيرا من عوامل التشغيل مثل طول المنتج - توصيلية المحلول الالكتروليتي - درجة الحرارة للمحلول - غاز الهيدروجين وتأثيره على التوصيلية - ضغط المحلول .

من خلال اكثر من ٢٠٠ تجربة معملية تمت مقارنة النتائج مع الدراسة النظرية المقترحة واطهرت المقارنة توافقا قويا بلغ حتى ١٠ ميكرونات فى بعض النتائج وذلك تحت ظروف التشغيل المختلفة واطهر البحث كذلك ان الخطأ الشكلي تصل قيمته حتى ٤٠ ميكرون لمنتج طولة ٤٠مم مما يؤيد اهمية حساب هذا العامل فى تكاملية الدقة لعملية التشغيل الكهروكيميائي ويوضح البحث كذلك الشكل التتابعى لتكون سطح المنتج خلال فترات زمنية متتالية واثر العوامل السابق ذكرها على قيمة الانحراف الشكلي .