



Final-Term Exam of (Electrical Machines III)  
For 4<sup>th</sup> Grad Electrical Engineering Dept. students.

Answer All Questions – Assume any missing data:

**First Question:** (8 + 8 + 8 Marks)

- a) A 3-phase, 4-pole, 50 Hz, star-connected synchronous machine has an armature with diameter of 0.5 m and length of 0.3 m. The equation for flux density distribution is:

$$B = 0.15 \sin \theta + 0.03 \sin 3\theta + 0.02 \sin 5\theta \text{ wb/m}^2$$

Double layer winding is used for the armature which has 60 coils with 10 turns per coil, 60° phase spread, and a span of 13/15 of a pole pitch. **Determine** the generated voltage between terminals.

- b) **Calculate** the specific iron loss in a specimen of alloy steel for a maximum flux density of 3.2 Wb/m<sup>2</sup> and a frequency of 50 Hz, using 0.5 mm thick sheets. The resistivity of alloy steel is  $0.3 \times 10^{-6} \Omega\text{m}$ . The density is  $7.8 \times 10^3 \text{ Kg/m}^3$ . Hysteresis loss in each cycle is 400 J/m<sup>3</sup>.

- c) A turbo-alternator runs on test at a continuous rated load of 30 MVA with a lagging power factor of 0.8. The following cooling air measurements are taken:

Volume of cooling air measured at intake = 30 m<sup>3</sup>/sec,

Intake air temperature = 15°C,

Outlet air temperature = 45°C,

Barometric reading = 750 mm of mercury.

- (i) **Find** the efficiency of the machine, taking the specific heat of air at constant pressure as 1000 J/Kg.°C, and the volume of 1 Kg of air is 0.78 m<sup>3</sup> at 0°C and a pressure of 760 mm mercury.

- (ii) **Estimate** the amount of cooling water in liter/sec to cool the air, assuming the temperature rise of water to be 8°C.

**Second Question:** (8 + 8 + 8 + 8 Marks)

- a) **Discuss** the cooling methods adopted for the following transformers:

i) Dry type.

ii) Oil immersed type.

- b) **Explain** the types of transformer tap changer, and **State** the reasons of providing transformer tapping on the high voltage windings?

- c) **Explain** and **analyze** the methods adopted for securing uniform surge voltage distribution over transformer windings?

- d) **Deduce** the condition to design a transformer for minimum volume?

**Third Question:** (15 + 15 Marks)

- a) **Calculate** the main dimensions and winding details of a 100 KVA, 2000/400 V, 50 Hz, single phase shell type, oil immersed, self-cooled transformer. Assume: voltage per turn 10 V, flux density in core and limb 1.1 Wb/m<sup>2</sup>, current density 1.4 A/mm<sup>2</sup>, window space factor 0.33. The ratio of window height to window width = 3; and ratio of core depth to width of central limb = 2.5. The stacking factor is 0.9.

- b) A single phase, 400 V, 50 Hz, transformer is built from stampings having a relative permeability of 1000. The length of flux path is 2.5 m, the area of cross section of the core is  $2.5 \times 10^{-3} \text{ m}^2$  and the primary winding has 800 turns. *Estimate* the maximum flux and no-load current of the transformer. The iron loss at working flux density is 2.6 w/kg. specific iron weigh =  $7.8 \times 10^3 \text{ kg/m}^3$ . Staking factor is 0.9.

**Fourth Question: (12 + 12 Marks)**

- a) *Prove* that: The output equation of a "m" phase synchronous generator can be expressed as:

$$Q = C_o \cdot D^2 \cdot L \cdot n_s$$

What is the main aim of applying this output equation?

- b) The design details of two d.c. machines A and B are tabulated below. *Compare* their relative outputs.

Machine	Diameter, D [m]	Core length, L [m]	Speed n, [r.p.s]	Slots, S	Area of each slot, $A_s$ [ $\text{mm}^2$ ]	Slot space factor, $S_f$	$B_{av}$ [ $\text{Wb/m}^2$ ]	Current density, $\delta$ [ $\text{A/mm}^2$ ]
A	0.75	0.31	10	72	48×11	0.5	0.6	4.5
B	0.55	0.25	7.5	61	44×10	0.43	0.56	5.2

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*Good Luck, Dr. Mohamed Eid.*

**2-3)** For a compound d.c generator, **deduce** the conditions that the machine can be operate as: under, flat, and over cumulative compound generator.

**2-4) Compare** between metadyne transformer, metadyne generator, and amplidyne generator, then **Derive** the formula that describe the voltage amplification factor of metadyne/amplidyne generator.

**Question № (3): (5 + 5 + 5 + 5 Marks)**

**3-1)** For a cylindrical synchronous generator, **deduce** the relation between the reactive power and power angle,  $Q = f(\delta)$ , then **explain** the effect of the excitation on the generator operating point.

**3-2)** One important parameter of synchronous alternator is short-circuit ratio, **explain** how it can be estimated, then **discuss** its influence on the operating characteristics and the physical size of a synchronous alternator?

**3-3)** From the phasor diagram of a salient-pole synchronous motor working at a power factor lagging, **derive** the following relations:

$$\tan(\theta - \delta) = \frac{V_t \sin \theta - I_a X_q}{V_t \cos \theta - I_a r_a}; \quad \text{and} \quad jE_f = V_t \cos \delta - I_a r_a \cos(\theta - \delta) - jI_d X_d$$

Where  $\delta$ ,  $\theta$  are load and power factor angles respectively.

**3-4)** A 2-pole, 3-phase, star-connected, cylindrical synchronous machine has the following parameters:

Armature synchronous inductance,  $L_s = 0.01\text{H/phase}$ , negligible armature resistance.

Field self-inductance,  $L_f = 30\text{ H}$ , Field winding resistance,  $r_f = 20\ \Omega$ .

Maximum field to armature mutual inductance  $M_{af-\max} = 0.5\text{ H}$

The machine is working as a generator at rated speed, delivers power to a balanced load at unity

P.F. Field windings is energized from 200 V dc source. If the voltage across the load terminals is

900 V/phase, **compute** the electrical output power.

**Question № (4): (10 + 10 + 10 Marks)**

**4-1)** From the primitive equivalent model of a three-phase induction machine, **prove** that the electromagnetic develop torque,  $T_e$  is given by:

$$T_e = \text{Re}(j2M I_2^* I_1)$$

Where,  $I_1$  : is stator current,  $I_2$  : is rotor current, and  $M$  : is stator to rotor mutual inductance.

**4-2) Explain** the performance of the induction motor under the following operating cases:

- i) Variable voltage, constant frequency,
- ii) Constant voltage, variable frequency, and
- iii) Variable voltage, variable frequency.

**4-3)** A three-phase cage induction motor operates at its rated voltage and frequency and has a rotor copper loss at maximum torque equals to 9 times that at full-load torque and has a slip of 3 % at full-load. Neglecting stator resistance and rotational losses, **calculate**:

- i) The maximum torque and its corresponding slip, and
- ii) The starting torque. Express the torques in terms of full-load torque.

