



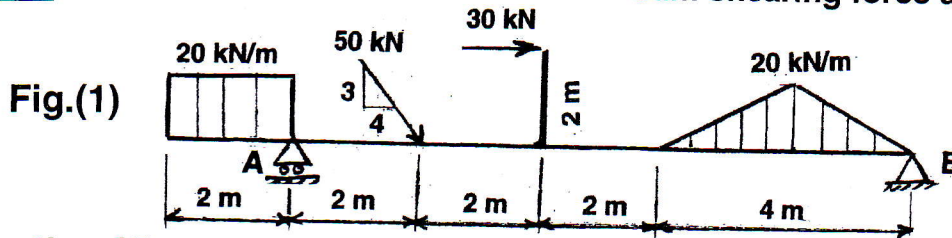
Allowed Tables and Charts: None - (take $g_0 = 9.8 \text{ m/s}^2$)

Examiner: Dr/ Mohamed Hesham Belal

Answer All the Following Questions:

Question (1): [15 Marks]

For the shown loaded beam in Fig.(1): 1)- Draw the internal action diagrams, and 2)- Find the values and locations of the maximum shearing force and bending moment.



Question (2): [20 Marks]

(a) [8 marks]—The 3000 kg anvil A for a drop forge is mounted on a nest of heavy coil springs having a combined stiffness of 2.8 MN/m. The 600 kg hammer B falls 500 mm from rest as shown in Fig.(3) and strikes the anvil which suffers a maximum deflection of 24 mm from its equilibrium position. Determine: (1)- the height (h) of rebound of the hammer, (2)- the coefficient of restitution (e) which applied, and (3)- the percentage loss of kinetic energy due to the impact.

(b) [12 marks]— An artificial satellite is launched in a direction parallel to the surface of the earth from a position (A) at an altitude h_0 . The trajectory of the satellite is elliptical orbit with maximum altitude h_1 at the position (B) as shown in Fig.(4). At the position (B) set of auxiliary rockets are fired to increase its velocity and set it in a parabolic orbit .

Given: $h_0 = 1.6 \times 10^6 \text{ m}$, $h_1 = 25.6 \times 10^6 \text{ m}$, $R = 6.4 \times 10^6 \text{ m}$.

Determine: (1)- the eccentricity and the semi latus rectum of the elliptical orbit, (2)- the periodic time of the elliptical orbit, (3)- the distance from the earth's center and the velocity of the satellite in the elliptical orbit at the position (C) , and (4)- the sudden change in the velocity at the position (B).

Question (3): [15 Marks]

(a) [8 marks]— The water flow enters the elbow through the fixed pipe joint at A at the rate of $0.2 \text{ m}^3/\text{s}$ and then discharged from the outlet at B as shown in Fig.(4). The static gauge pressure at A is 100 kPa and the density of water is 1000 kg/m^3 . The water-filled elbow has a mass of 20 kg and center of mass at C. The diameter of the inlet pipe at A is 0.2 m, and the diameter of the outlet at B is 0.1 m.

Determine the horizontal and vertical force reactions and the moment reaction on the fixed pipe joint at A.

(b) [7 marks]— A horizontal shaft with a flywheel of mass 32 kg and a radius of gyration of 0.5 m about its mass center starts to rotate under the action of a driving moment $M = M_0 - C\theta$, as shown in Fig.(5), where the constants $M_0 = 1000 \text{ N.m}$ and $C = 8 \text{ N.m/rad}$. (1)- Derive the equation of motion and then the relationship between the angular velocity and angular displacement ($\omega - \theta$ relation),

(2)- Calculate the number of revolutions executed by the flywheel before stopping.

Question (4):

[25 Marks]

(a) [13 marks] — The vibratory system shown in Fig.(6) has the natural frequency equal 30 rad/s and the following data: $m_1 = 10$ kg, $m_2 = 16$ kg, $J_0 = 6.4$ kg.m², $a = 40$ cm, $b = 80$ cm, $k_1 = 2k_2$. When the system was displaced and released, the amplitude of any cycle decreases to 0.25 of the value of previous cycle.

- (1)- Find the values of unknowns C , k_1 and k_2 , (2)- Find the periodic time,
 (3)- When the mass m_1 is subjected to a harmonic force: $F(t) = 540 \sin 60t$ N, write down the equation of motion, and determine the steady state response.

(b) [12 marks] —The thin circular disk of mass $m = 2$ kg and radius $r = 20$ cm is mounted on a shaft with length $R = 50$ cm. The disk rotates about its own z-axis with a constant angular velocity $\omega_2 = 30$ rad/s. Simultaneously, the frame is rotating about the Z-axis at constant angular velocity $\omega_1 = 12$ rad/s with a fixed angle $\theta = 60^\circ$ as shown in Fig.(7). Axis z has the momentary orientation above Y-axis of the fixed axes X-Y-Z. Determine: (1)- the angular velocity and angular acceleration of the disk, (2)-the velocity and acceleration of point A on the rim of the disk, (3)-the total reaction at the support of the shaft, and (4)- the variation in the dynamic reaction if the nutation angle changed to 90° .

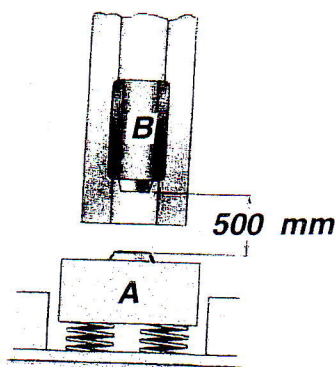


Fig.(2)

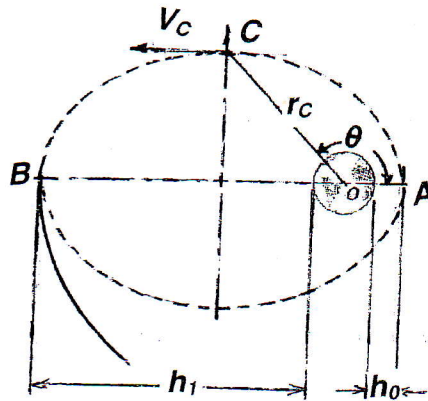


Fig.(3)

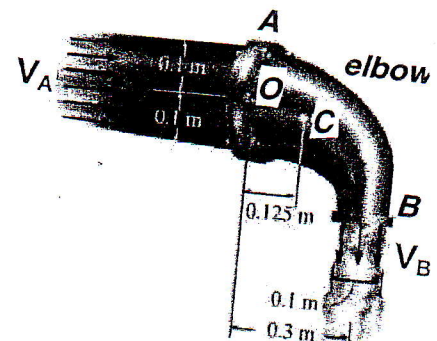


Fig.(4)

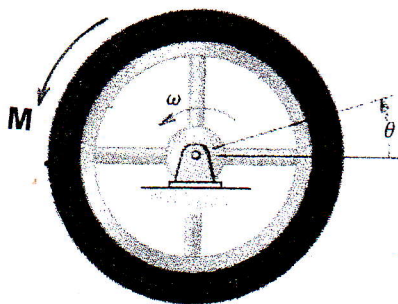


Fig.(5)

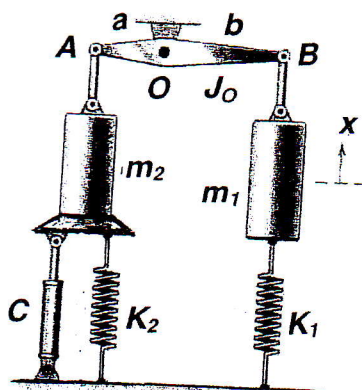


Fig.(6)

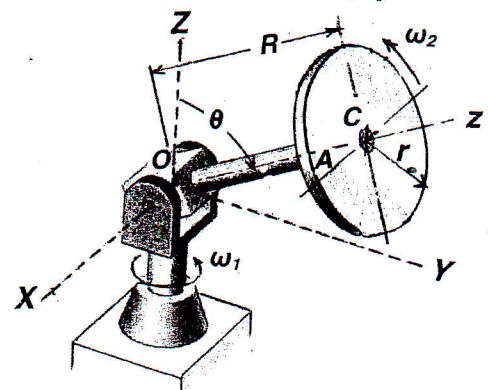


Fig.(7)

With my best wishes

This exam measure the following ILOs												
Question No.	Q1	Q2-a	Q3-b	Q4-b	Q1	Q2-a	Q3-b	Q4-a	Q1	Q2-b	Q3-a	Q4-a
	a-1	a-4	a-1	a-4	b-2	b-7	b-7	b-2	C1	C1	C1	C1
Skills	Knowledge & Understand				Intellectual				Professional			