

Answer the following questions

Q1: (25 Marks)

Determine each of the following:

1. The equivalent mass of the lever shown in figure (1-a) at point (A) if:
 $m_1 = m_2 = m_3 = 5 \text{ Kg}$ and $l_1 = 5, l_2 = 10, l_3 = 15 \text{ m}$.
2. The equivalent moment of inertia of the rack and pinion arrangement shown in figure (1-b) if:
 $m = 20 \text{ Kg}$, $R = 200 \text{ mm}$ and the radius of gyration = R .
3. The equivalent stiffness of the boom shown in figure (1-c) if:
 Young's modulus of material $E = 2.1 \times 10^{11} \text{ N/m}^2$
 Lengths $l_1 = l_2 = l_3 = 3 \text{ m}$.
 Cross sectional areas $A_1 = 20 \text{ cm}^2$, $A_2 = 10 \text{ cm}^2$, $A_3 = 5 \text{ cm}^2$

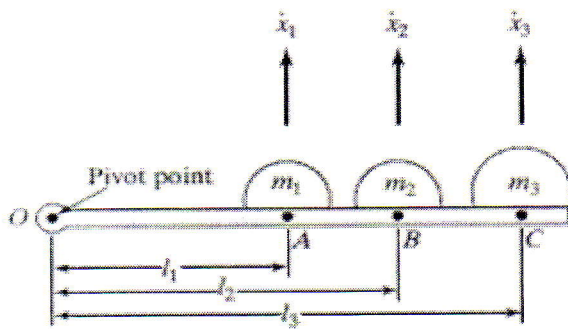


Figure (1-a)

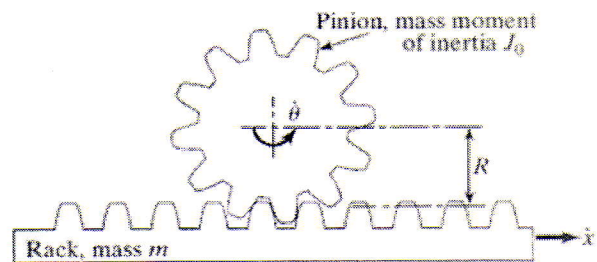


Figure (1-b)

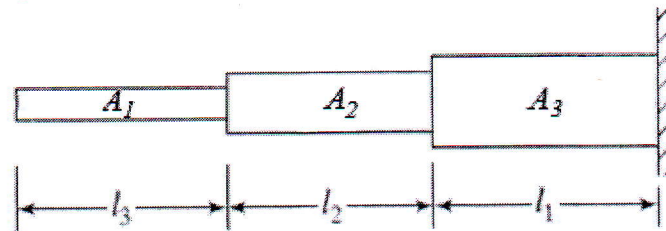


Figure (1-c)

Q2: (25 Marks)

If the mechanical system shown in figure (2) is subjected to a periodic force in the form: $f(t) = \frac{a_0}{2} + \sum_{j=1}^{\infty} a_j \cos(j\omega t) + \sum_{j=1}^{\infty} a_j \cos(j\omega t)$.

Determine the equation of the time response, assuming zero initial conditions.

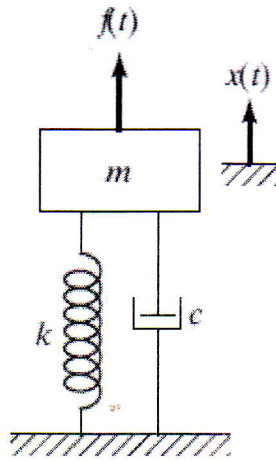


Figure (2) Mechanical System.

Q3: (25 Marks)

State the equations of motion of the system shown in figure (3).

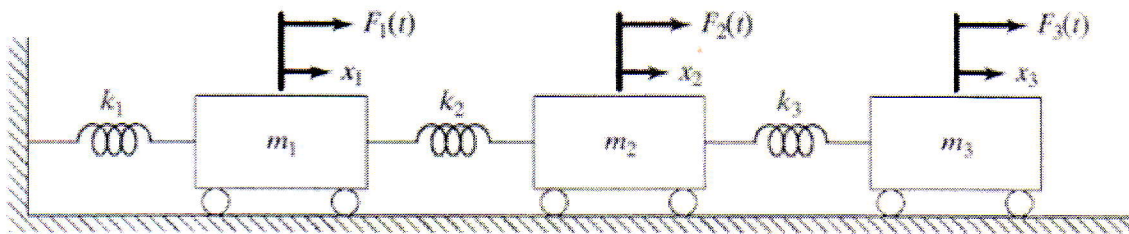


Figure (3) Un-damped Mechanical System.

If the masses $m_1 = m_2 = m_3 = m$ and the stiffnesses $k_1 = k_2 = k_3 = k$, find out the natural frequencies and mode shapes of the given system.

Q4: (25 Marks)

An electric motor of mass M , mounted on an elastic foundation, is found to vibrate with a deflection of 0.15 m at resonance. The unbalanced mass of the motor is 8% of the mass of the rotor and the damping ratio of the foundation is $\zeta = 0.25$, determine:

- the eccentricity of the unbalanced mass (e),
- the peak deflection of the motor when the frequency ratio varies from resonance, and
- the additional mass to be added uniformly to the motor if the deflection of the motor at resonance is to be reduced to 0.1 m.

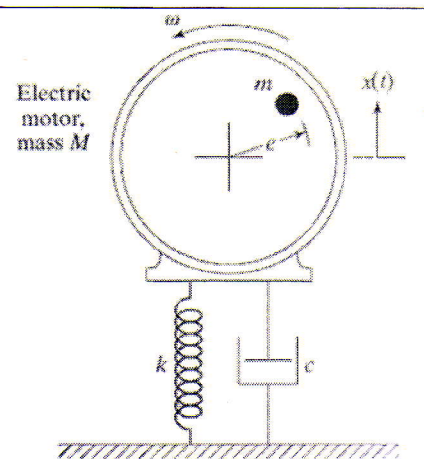


Figure (4)