



**Answer Only Five Questions**

**Question 1 : ( 24 marks )**

For the forced damped vibrating system shown in Fig. 1, neglecting the rotating of the rigid link 2 :

- Express the potential energy of the system at an arbitrary instant
- Express the kinetic energy of the system at an arbitrary instant.
- Express the dissipative energy of the system at an arbitrary instant.
- Write the system equation of motion by using Lagrange's equation.

**Question 2: ( 24 marks )**

A spring mass system of mass 20 kg, and spring stiffness 4000 N/m, vibrates in a viscous medium of coefficient 50 N.sec/m. If the initial amplitude is 20 mm, Find :

- The amplitude after 5 cycles,
- The damped natural frequency,
- The periodic time of damped oscillation.

**Question 3: ( 24 marks )**

A machine of mass  $M= 600$  kg is supported on springs with a static deflection of 60 mm and attached with a damper of  $c= 3000$  N.sec/m. If the machine has a rotating unbalance ( $me$ ) of 0.9 kg m, determine:

- The steady state amplitude at a speed 1200 rpm and the force transmitted to the foundation at this speed, and
- If the machine mounted on a large block of mass 400 kg and the static deflection of the springs is still 60 mm, what be the steady state amplitude.

**Question 4: (24 marks)**

A mathematical model of vibration pile driver is shown in Fig.2. The mass of gear box pile,  $m_1=4000$  kg and mass of yoke,  $m_2=1000$ kg. The stiffness of the connecting links  $k_2= 3000$  kN/m and helical spring  $k_3= 300$  kN/m. The soil into the pile driven having stiffness,  $K_1=600$  kN/m.

- If an exciting force of gear box  $F= 5000 \cos 100t$  N, derive the equation of motion, natural frequencies and mode shapes of the system.
- Compute the impedance matrix and hence estimate the amplitudes and displacement of the pile set and yoke.

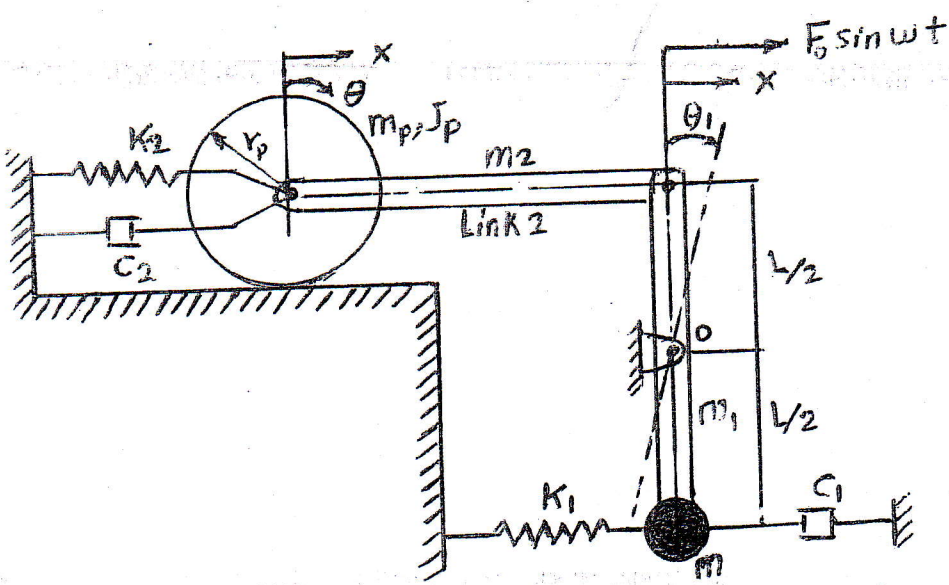


Fig. 1

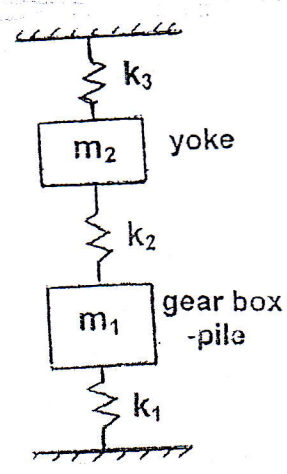


Fig. 2

Please see page no. (2)

**Question 5 (24 marks)**

A cantilever of longitudinal rigidity  $EA$ , mass density  $\rho$  and length  $L$  performs a longitudinal vibration. If the free end of the beam is fastened to a motor of mass  $m$  as shown in Fig. (3)

- (a) Derive the frequency equation of the present continuous system.
- (b) If ( $\rho = 0$ ) the beam becomes one degree of freedom system the motor having of 400 kg and an unbalance of 3 kg.cm. The beam is observed to vibrate with large amplitudes at the operating speed of 1200 r.p.m of the motor. It is proposed to add a vibration absorber to reduce the vibration of the beam. Determine the mass and stiffness of the absorber needed in order to have the lower frequency of the resulting system equal to 60% of the operating speed of the motor.

**Question 6 (24 marks)**

A rotating shaft with four unbalanced masses should be completely balanced by the two masses situated on the radius  $r_0$  in the two respective planes  $P_L$  and  $P_R$  as shown in Fig. 4. Find the magnitudes of these masses  $m_L$  and  $m_R$  and these angular locations  $\phi_L$  and  $\phi_R$ .  
 Given:  $m_1=10$  gm,  $m_2=15$  gm,  $m_3= 20$  gm,  $m_4= 25$  gm,  $a=10$  cm,  $r_1=25$  cm,  $r_2= 30$  cm  $r_3=10$  cm,  $r_4= 20$  cm,  $r_0= 20$  cm,  $\phi_1= 30^\circ$ ,  $\phi_2= 135^\circ$ ,  $\phi_3= 210^\circ$ ,  $\phi_4= 300^\circ$ .

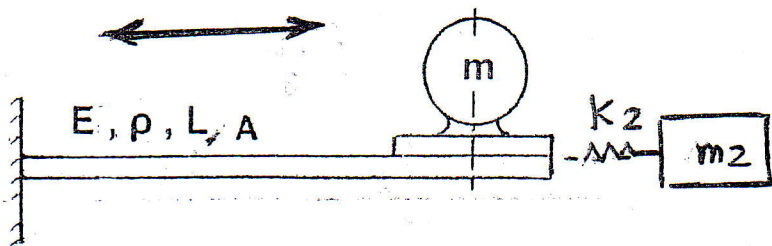


Fig. 3

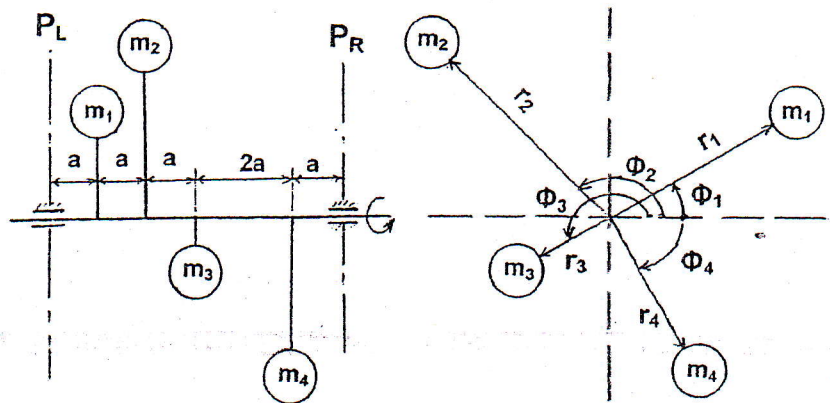


Fig. 4

*With our best wishes*

This exam measures the following ILOs

Question Number	1-(a-c)	1-d			4-a	4-b	5-a	5-b	2,6	2-1	3-11		
Skills	a-1	a-19			b17-1	b17-2	b17-1	b17-2	b17-2	c1	c1		
	Knowledge & Understanding Skills				Intellectual Skills				Professional Skills				